

# Regularised patient-specific stopping power calibration for proton therapy planning based on proton radiographic images

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**Proton radiography (2D)**

**Range accuracy**

**X-ray planning CT**

**Treatment planning**

**CT number to RSP conversion**

Physics in Medicine & Biology



PAPER

Regularised patient-specific stopping power calibration for proton therapy planning based on proton radiographic images

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Treatment planning software needs accurate knowledge about the **proton stopping power** in the patient:

$$S(x) = -\frac{dE}{dx}(E(x)) \quad \text{depends on proton energy}$$

Integration yields the protons' penetration depth, called **range**:

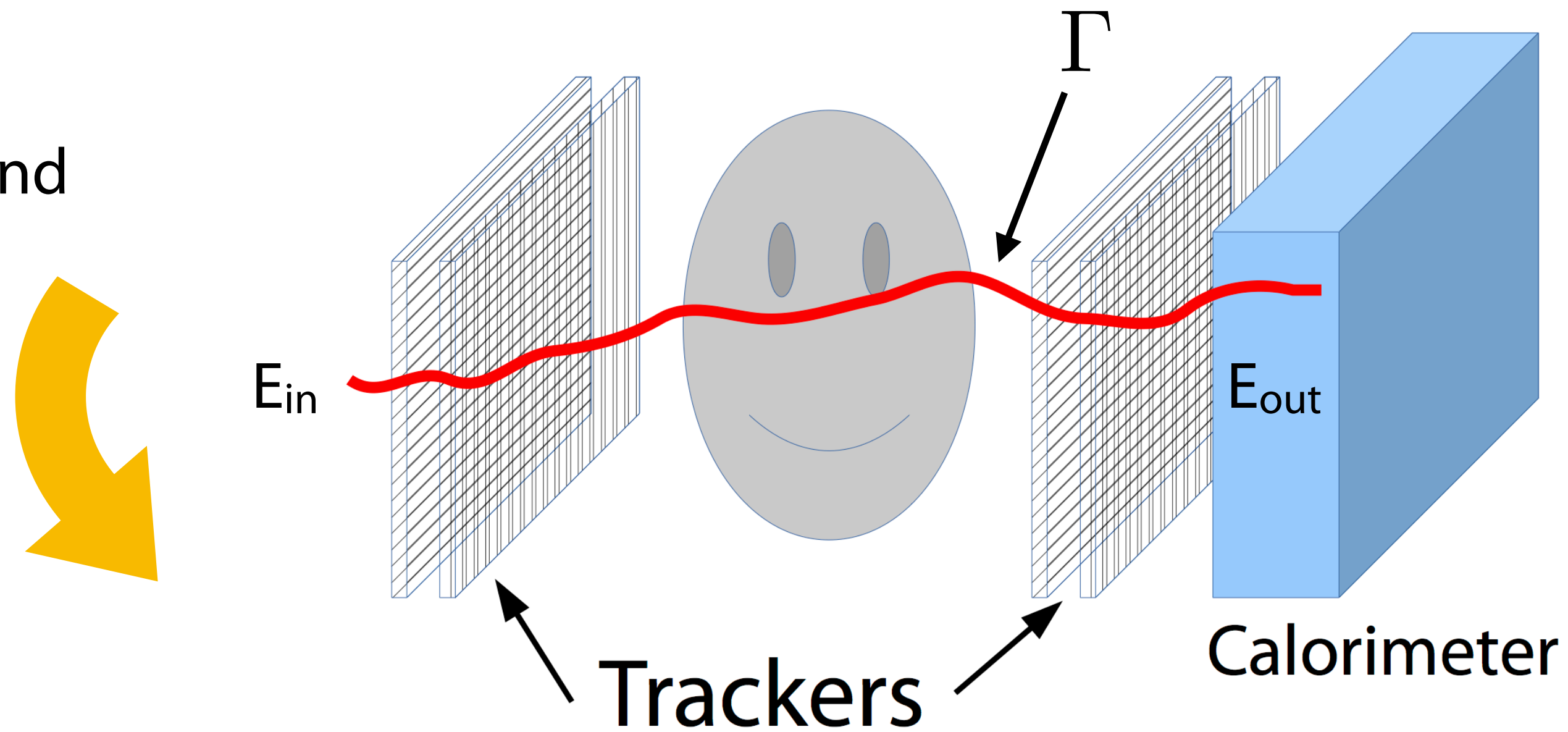
$$\text{Range} = \int_{E_{\text{final}}}^{E_{\text{in}}} \frac{dE}{\rho S(E)}$$

Convenient to define **Relative Stopping Power (RSP)** in reference to water:

$$RSP \equiv \frac{S(x)}{S_w(x)} \quad \text{approximately energy independent}$$

# Option 1: Get Stopping Power from proton CT

Rotate around patient



Generates list mode data:  
Trajectory estimate and  
WET for each proton.

Reconstruction formula for proton CT:

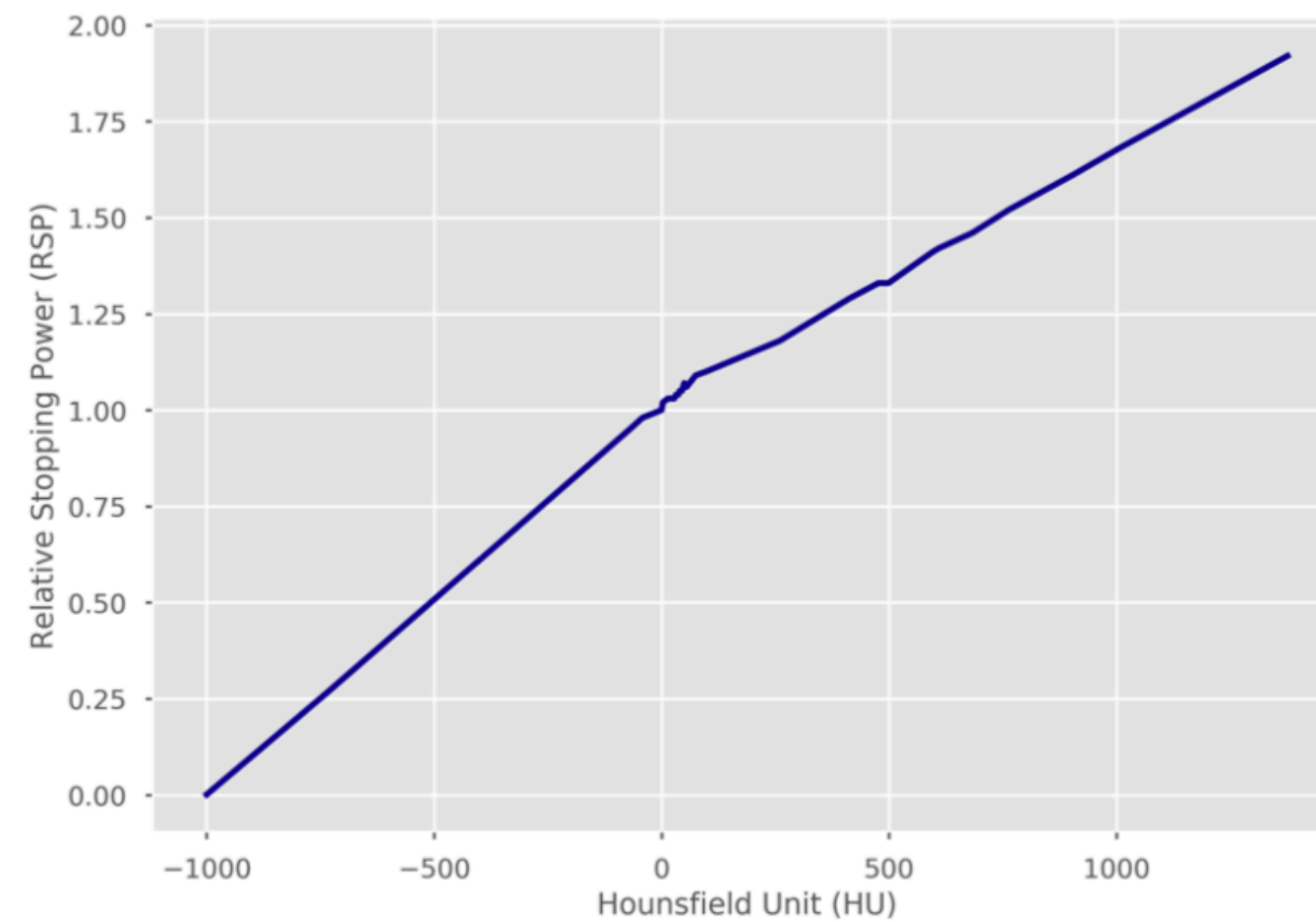
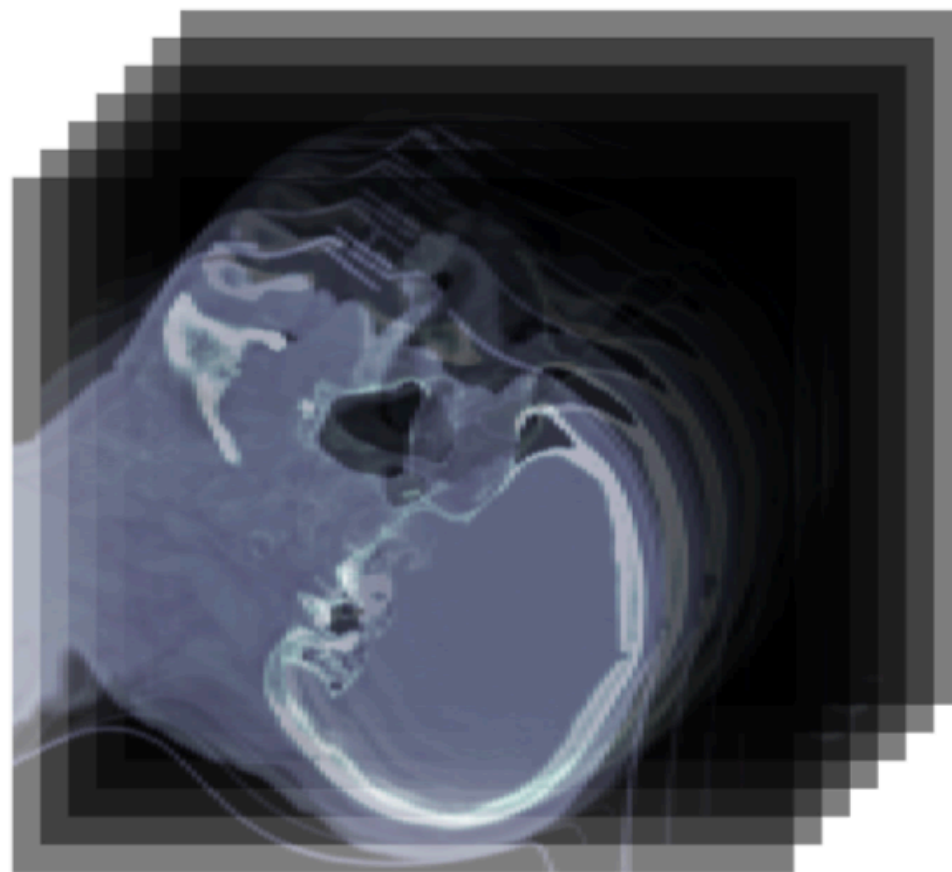
$$WET = \int_{\Gamma} RSP(x) dl = \int_{E_{out}}^{E_{in}} \frac{dE}{S_w(E)}$$

WET: water equivalent thickness

**Not used clinically.  
Only prototypes!**

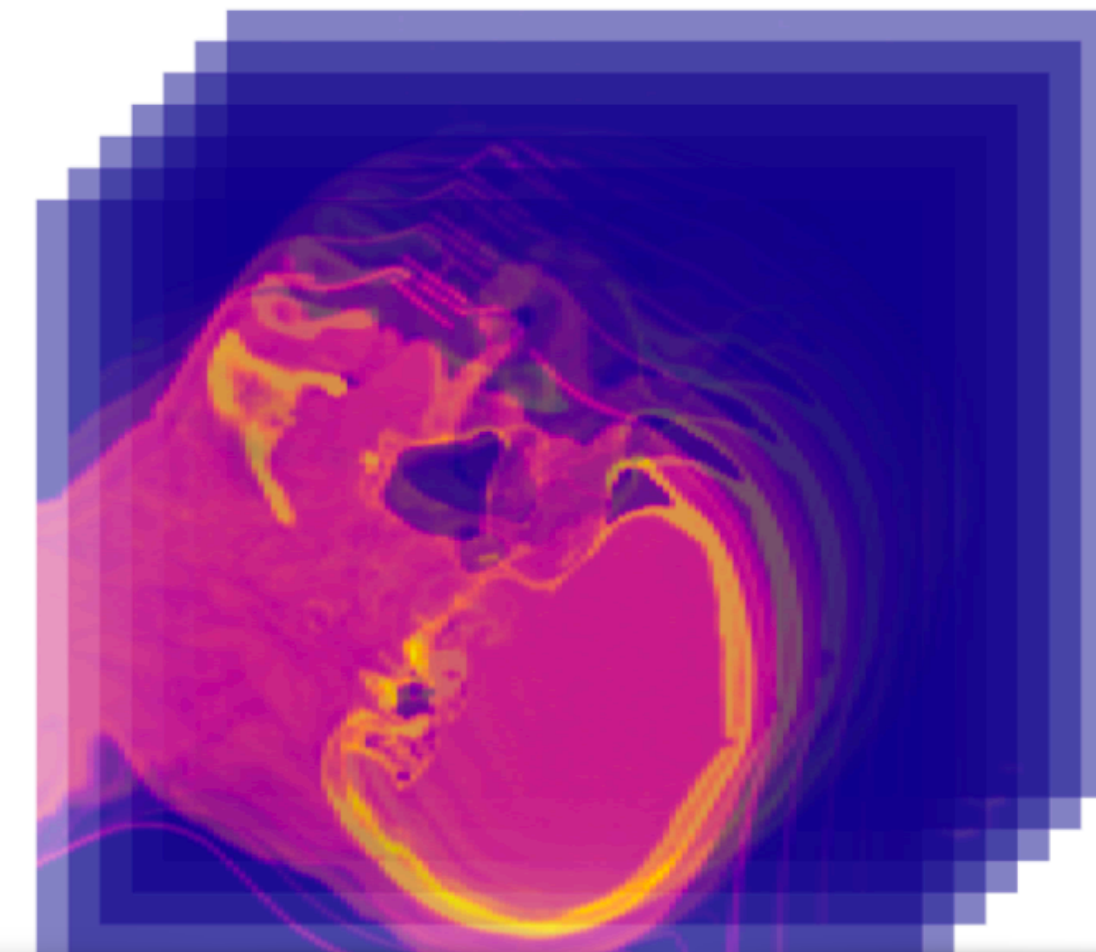
# Option 2: Use X-ray CT plus conversion (clinically used)

Planning CT



Conversion

Relative Stopping Power (RSP)



**Conversion depends on chemical tissue composition  
-> inter/intra patient variation**

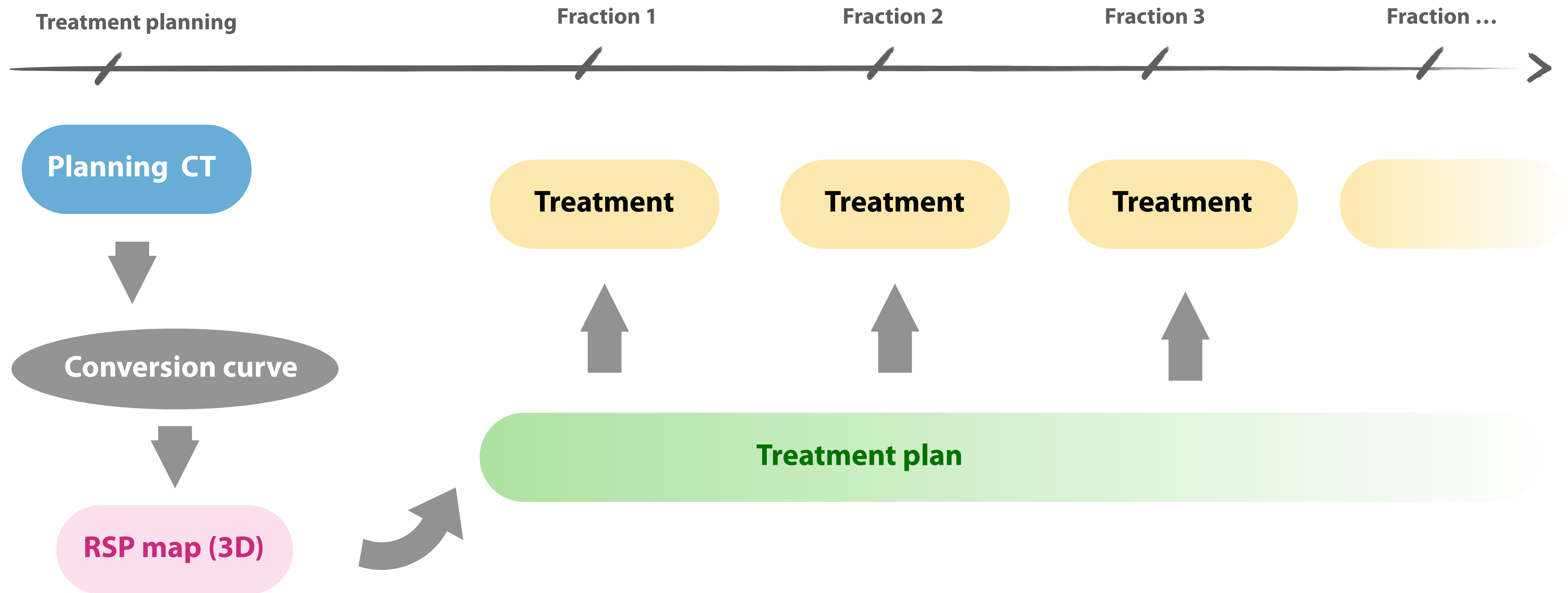
Uncertainties in

- Hounsfield Units (HU)
- Conversion curve

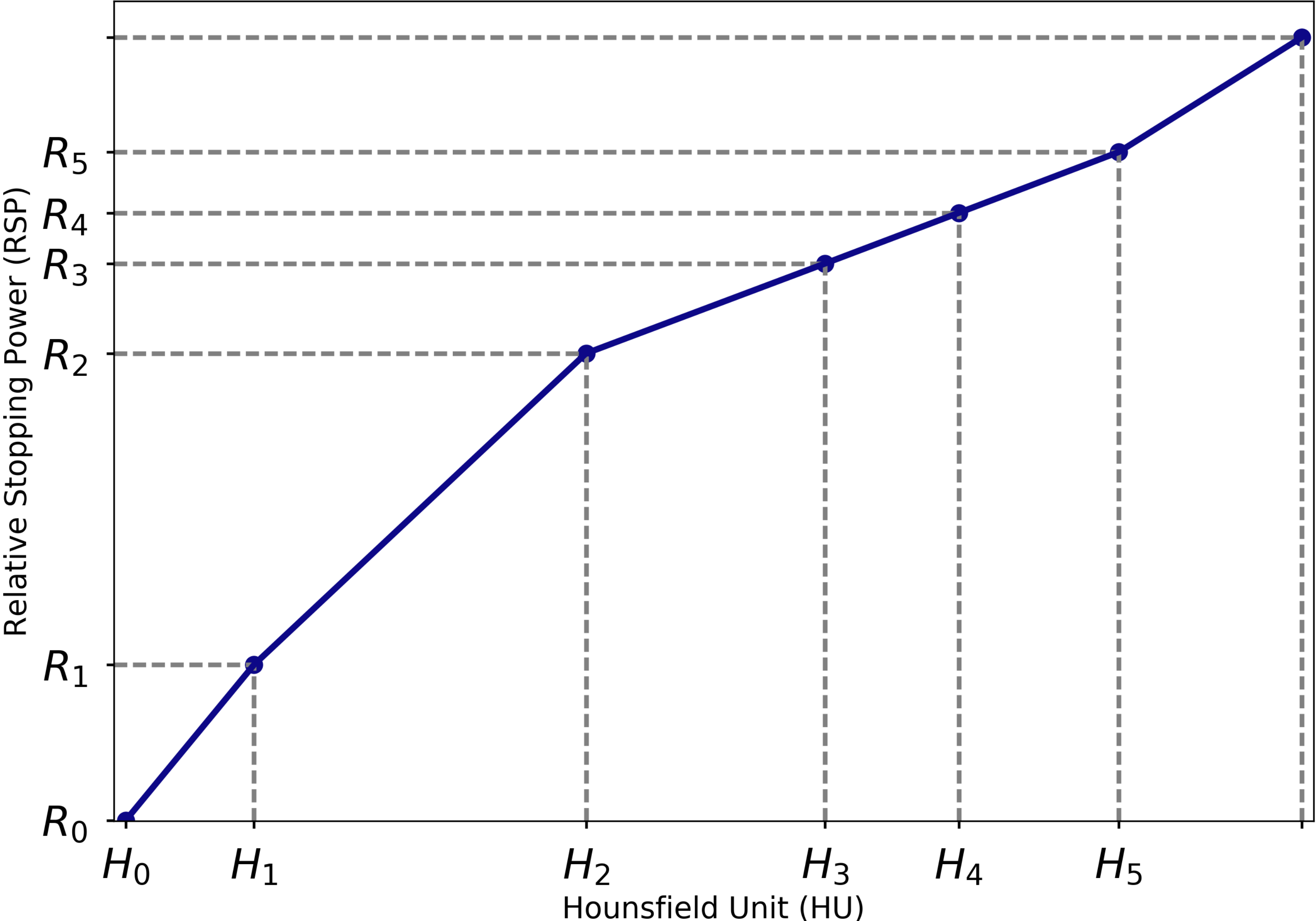


Range  
uncertainties

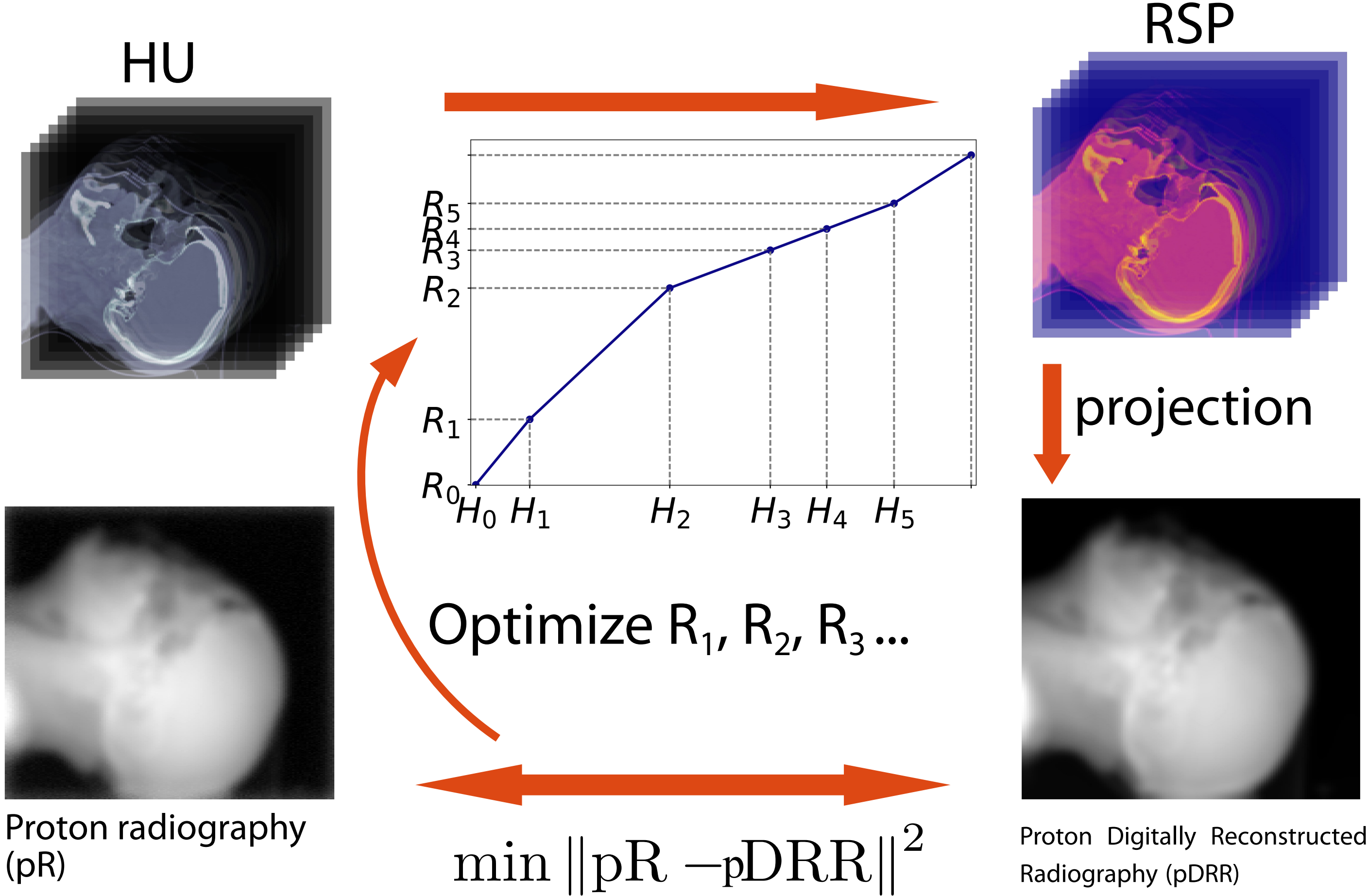
# Typical clinical workflow in proton therapy



# Goal: Find patient specific optimal conversion curve



# Patient specific CT-RSP calibration using proton radiography



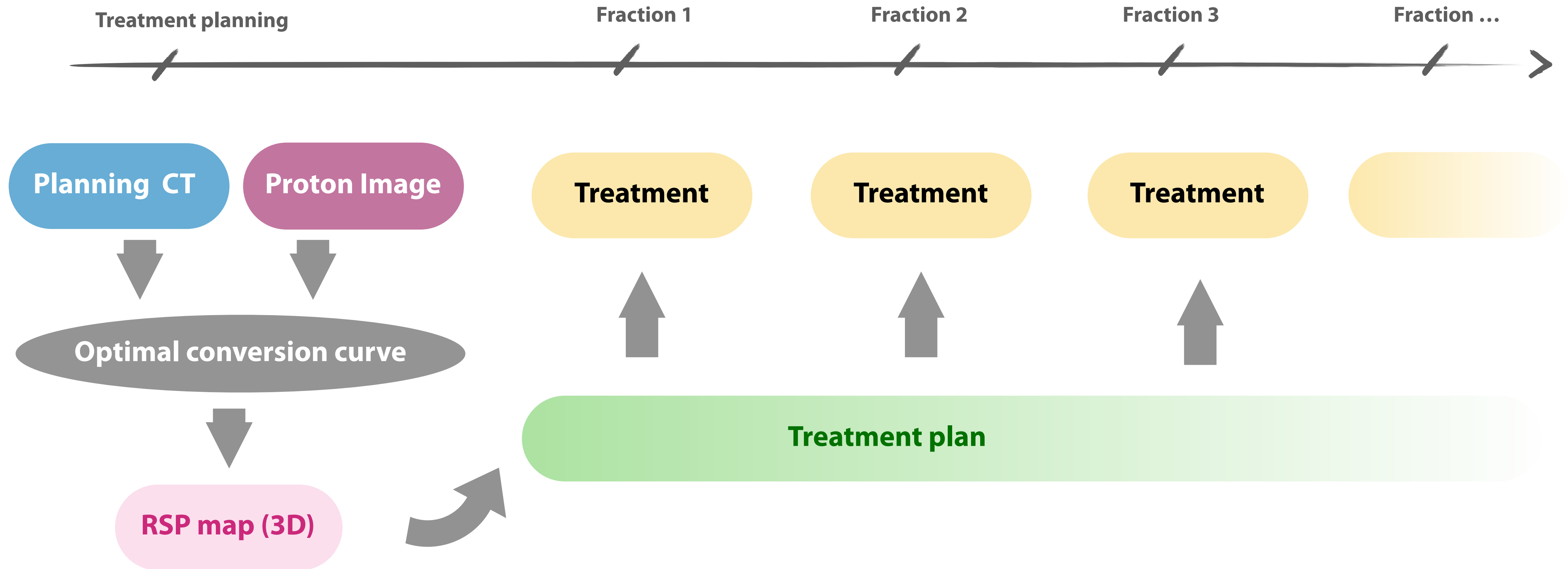
[1] Schneider, U. et al. (2004). First proton radiography of an animal patient. Medical Physics, 31(5)

[2] Doolan, P. J. et al. (2015). Patient-specific stopping power calibration for proton therapy planning based on single-detector proton radiography. PMB 60(5)

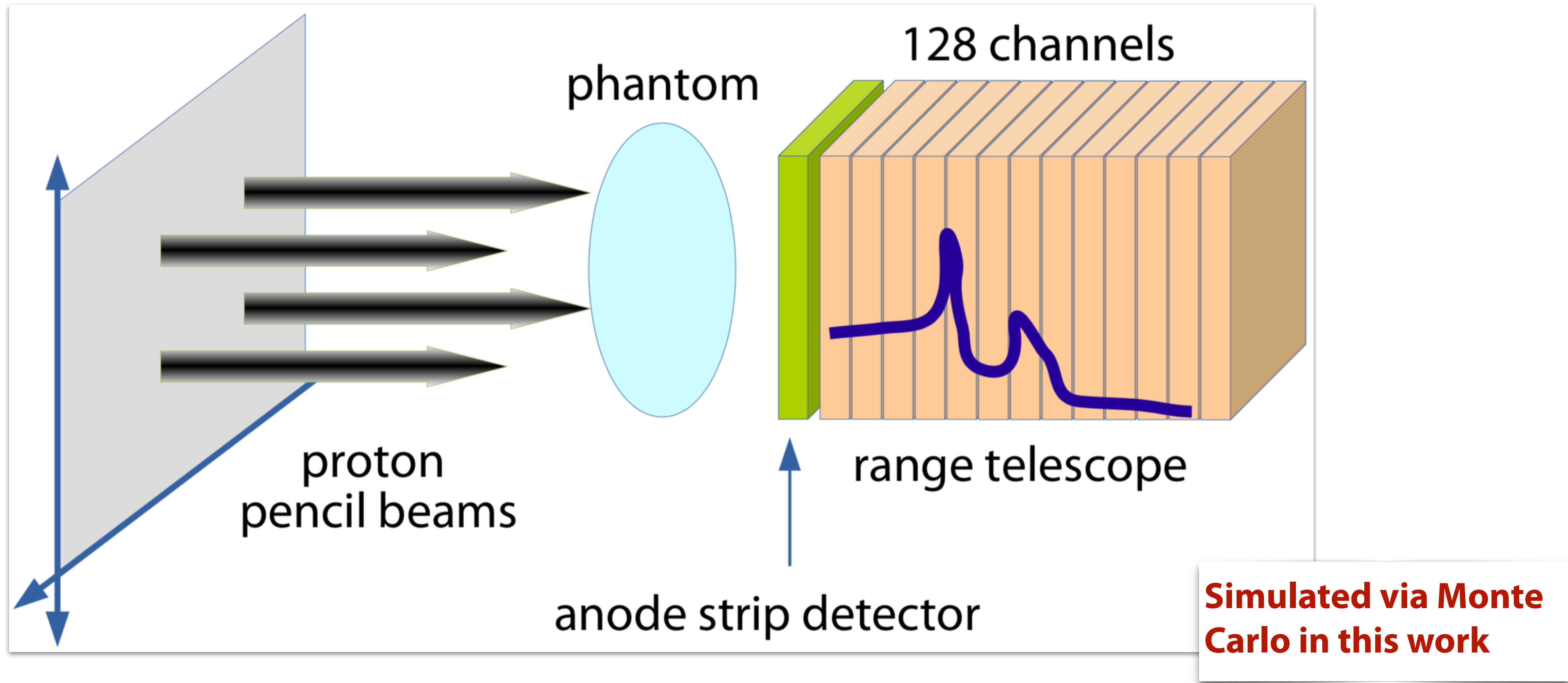
[3] Collins-Fekete, C.-A. et al. (2017). Pre-treatment patient-specific stopping power by combining list-mode proton radiography and x-ray CT. PMB 62(17)



# Modified clinical workflow

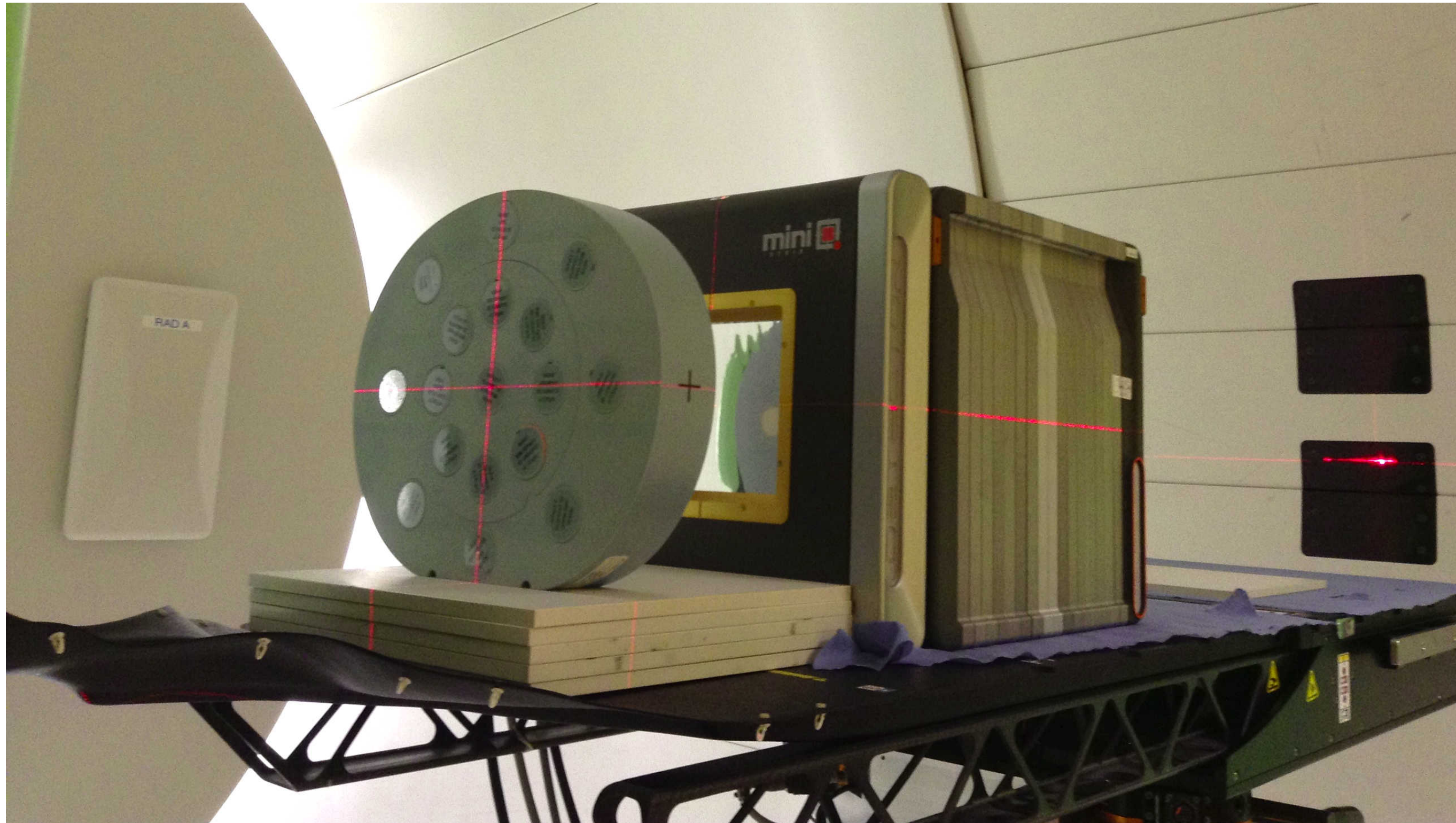


# Proton imaging system



# Example of a proton radiography system

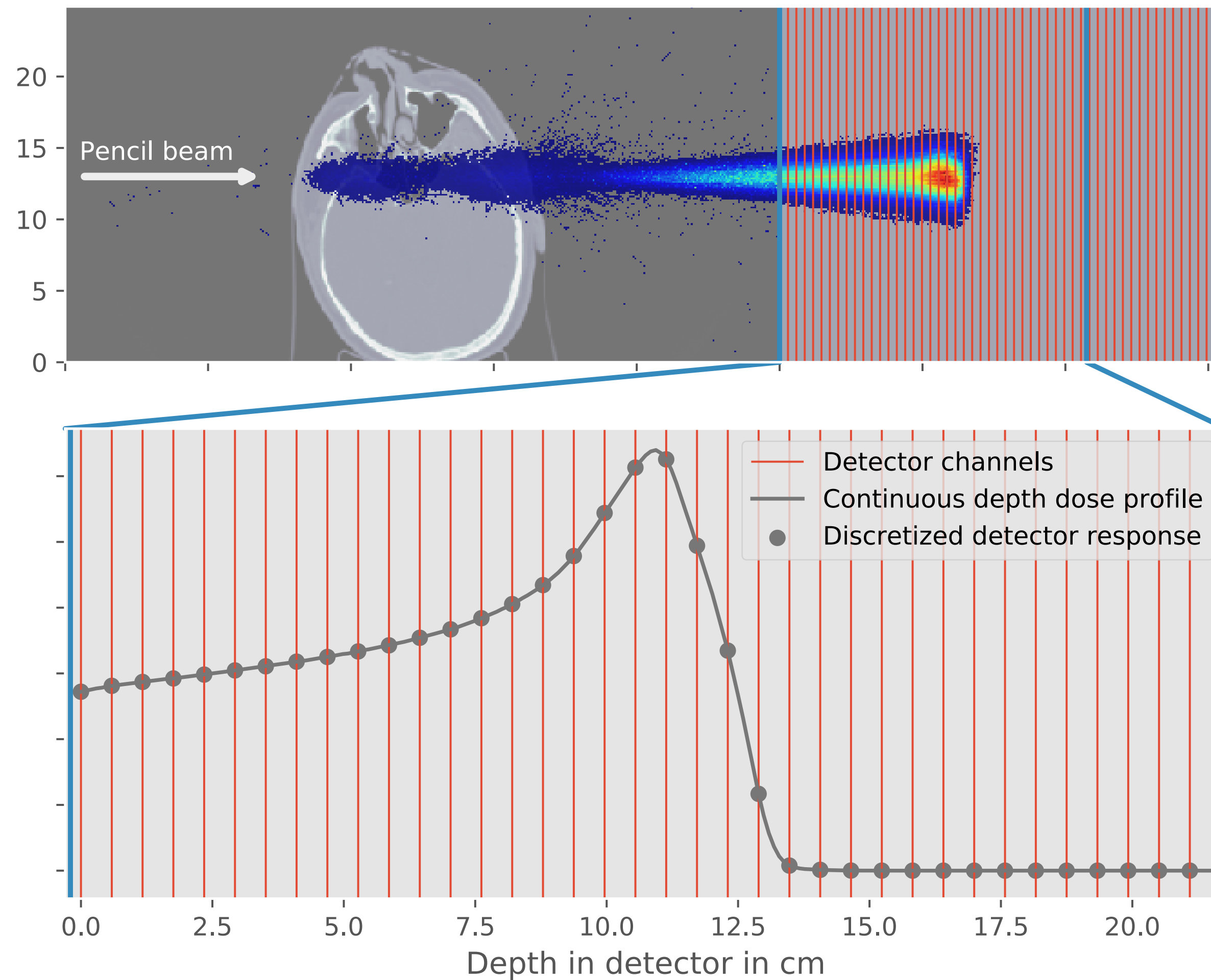
... used at CPO, France



... and Maastrro, Netherlands



# Monte Carlo simulation of proton radiographies

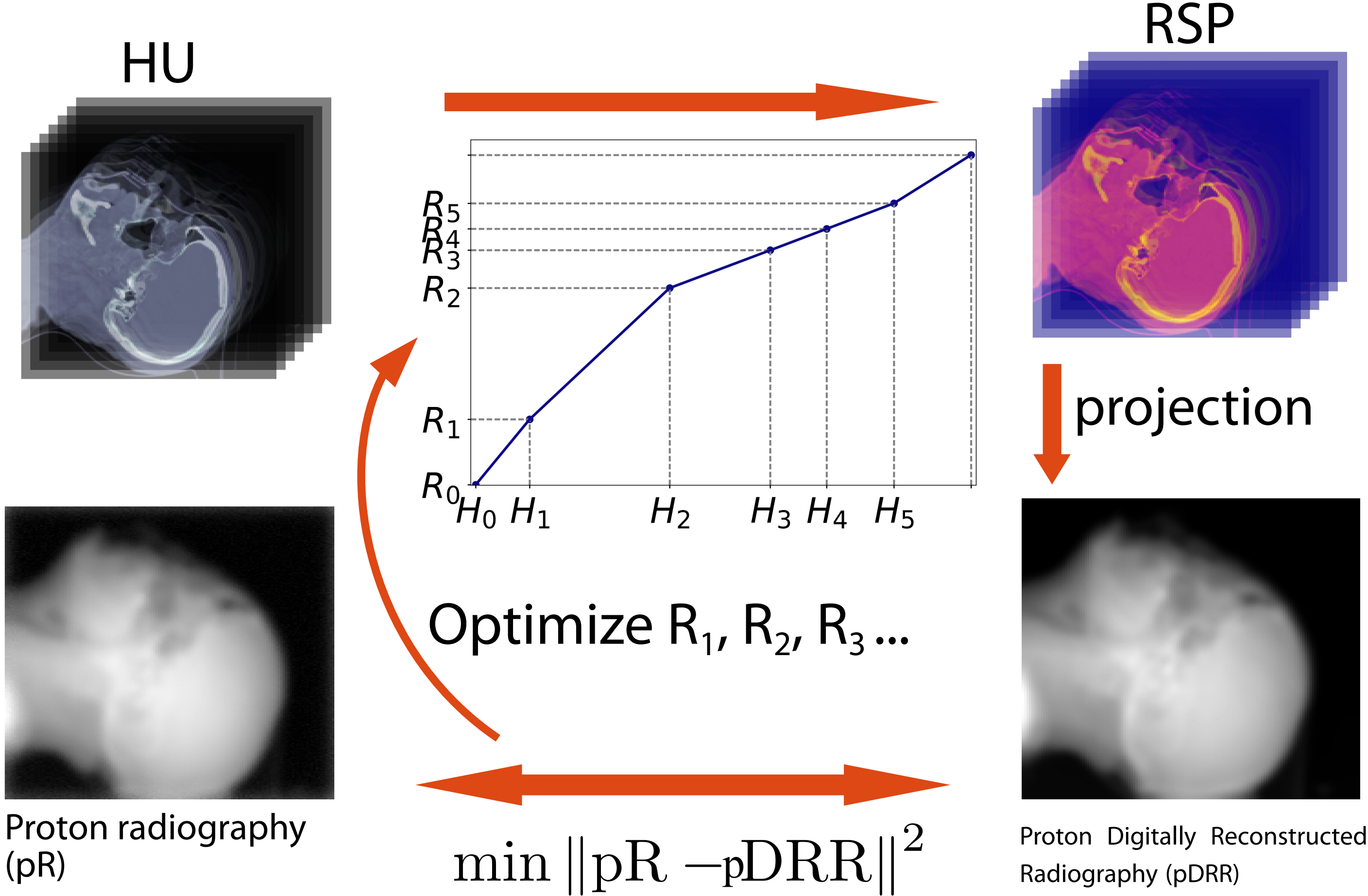


Used fast GPU-accelerated Monte Carlo code "Fred" developed at the University of Rome la Sapienza.

Takes 1-2 min per proton radiography.

Ground truth CT-RSP curve is the one used for the simulation.

# Patient specific CT-RSP calibration using proton radiography



[1] Schneider, U. et al. (2004). First proton radiography of an animal patient. Medical Physics, 31(5)

[2] Doolan, P. J. et al. (2015). Patient-specific stopping power calibration for proton therapy planning based on single-detector proton radiography. PMB 60(5)

[3] Collins-Fekete, C.-A. et al. (2017). Pre-treatment patient-specific stopping power by combining list-mode proton radiography and x-ray CT. PMB 62(17)

# Efficient implementation of projection (1)

In each voxel, replaces CT number  $h$  by weight vector  $w$ :

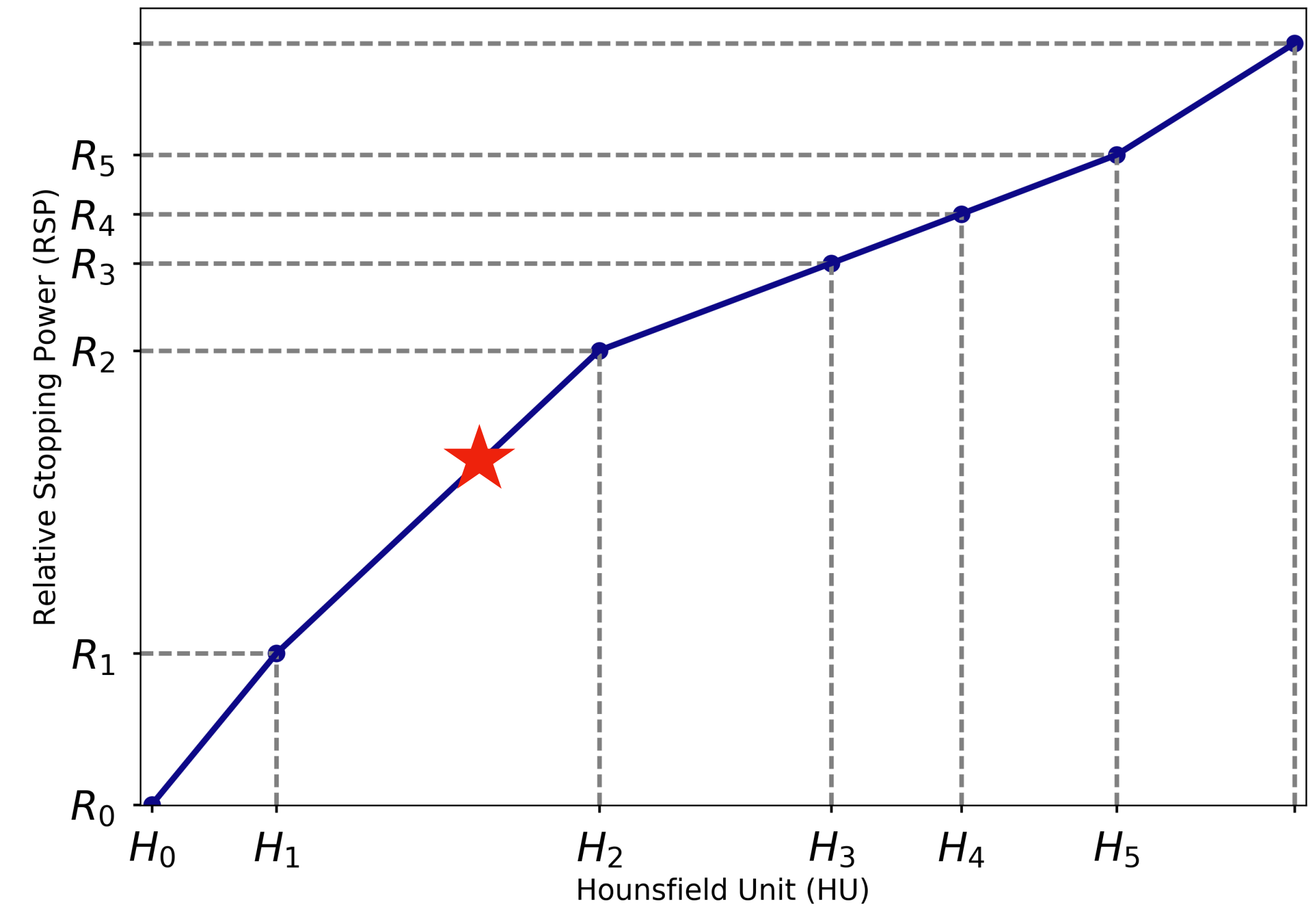
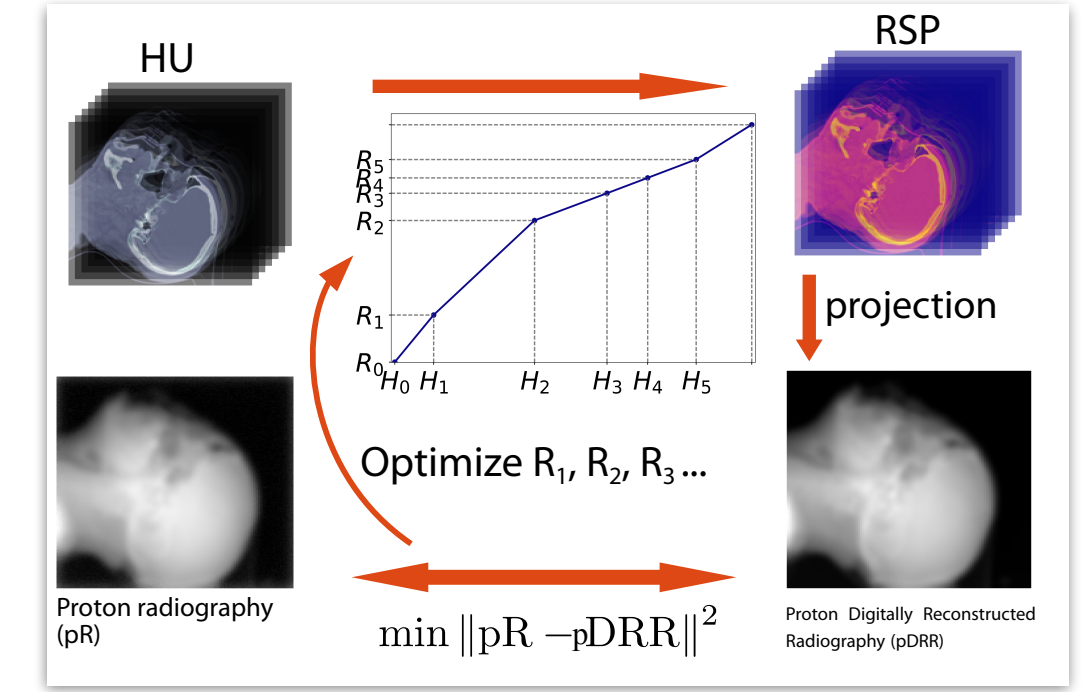
$$w_\alpha(h) \equiv \frac{h - H_{\alpha-1}}{H_\alpha - H_{\alpha-1}} \Omega_\alpha(h) + \frac{H_{\alpha+1} - h}{H_{\alpha+1} - H_\alpha} \Omega_{\alpha+1}(h)$$

$$w_0(h) = \frac{H_1 - h}{H_1 - H_0} \Omega_{\alpha=1}(h)$$

$$w_N(h) = \frac{h - H_{N-1}}{H_N - H_{N-1}} \Omega_{\alpha=N}(h)$$

with  $\Omega_\alpha(h) = \begin{cases} 1 & \text{for } H_{\alpha-1} \leq h < H_\alpha \\ 0 & \text{otherwise.} \end{cases}$

$$r = \sum_{\alpha=0}^N w_\alpha R_\alpha = \vec{w} \cdot \vec{R}$$



# Efficient implementation of projection (2)

3D RSP map is given by:

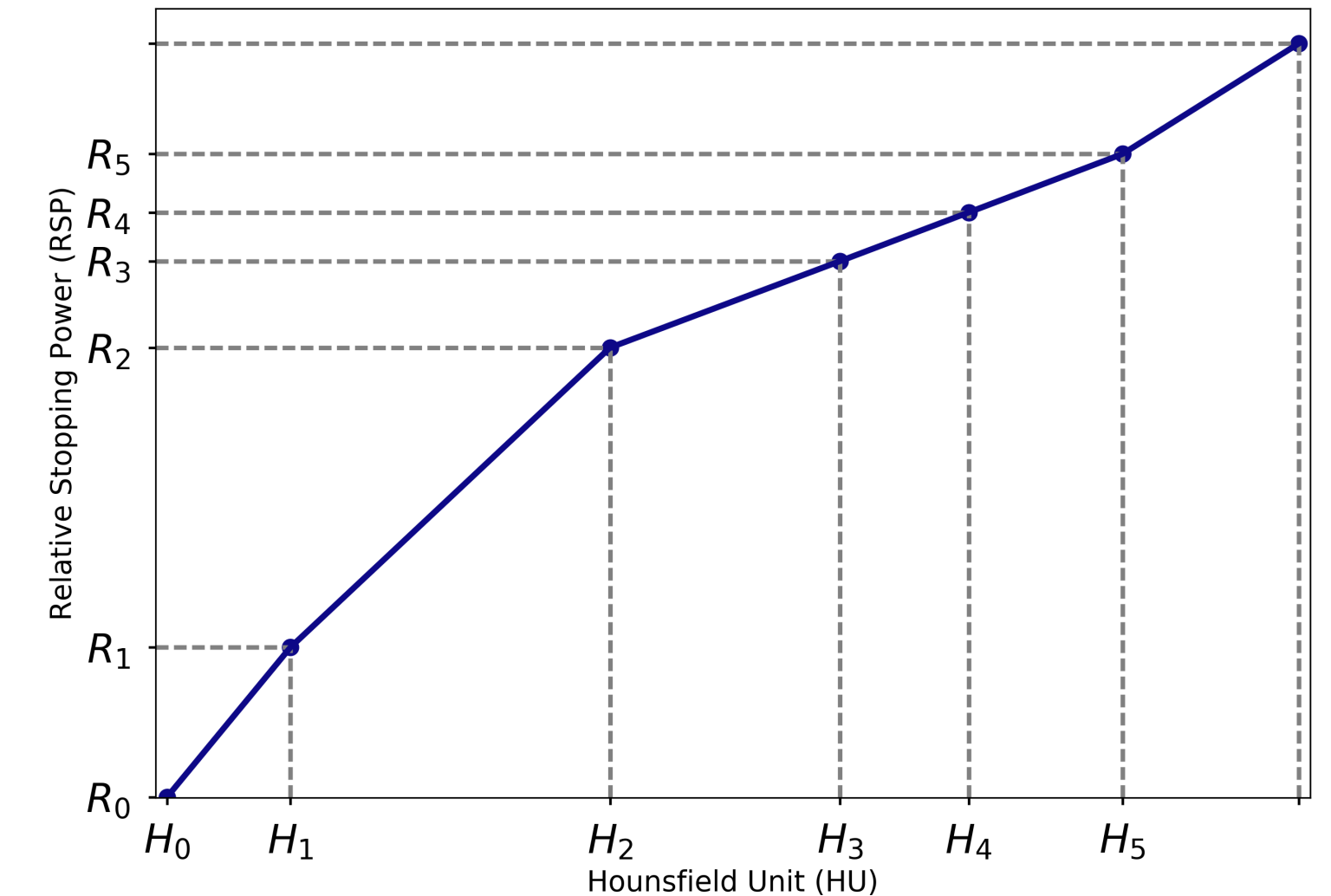
$$r_{ijk} = \sum_{\alpha=0}^N w_{ijk,\alpha} R_{\alpha} = \vec{w}_{ijk} \cdot \vec{R}$$

Proton digitally reconstructed radiography:

$$D_{i_p j_p} = \text{proj}_{k, i_p j_p} \left( \sum_{\alpha=0}^N w_{ijk,\alpha} R_{\alpha} \right) = \sum_{\alpha=0}^N \text{proj}_{k, i_p j_p} (w_{ijk,\alpha}) R_{\alpha} = \sum_{\alpha=0}^N A_{i_p j_p, \alpha} R_{\alpha}$$

$$\text{with } A_{i_p j_p, \alpha} = \text{proj}_{k, i_p j_p} (w_{ijk,\alpha})$$

**allows splitting projection from optimization**



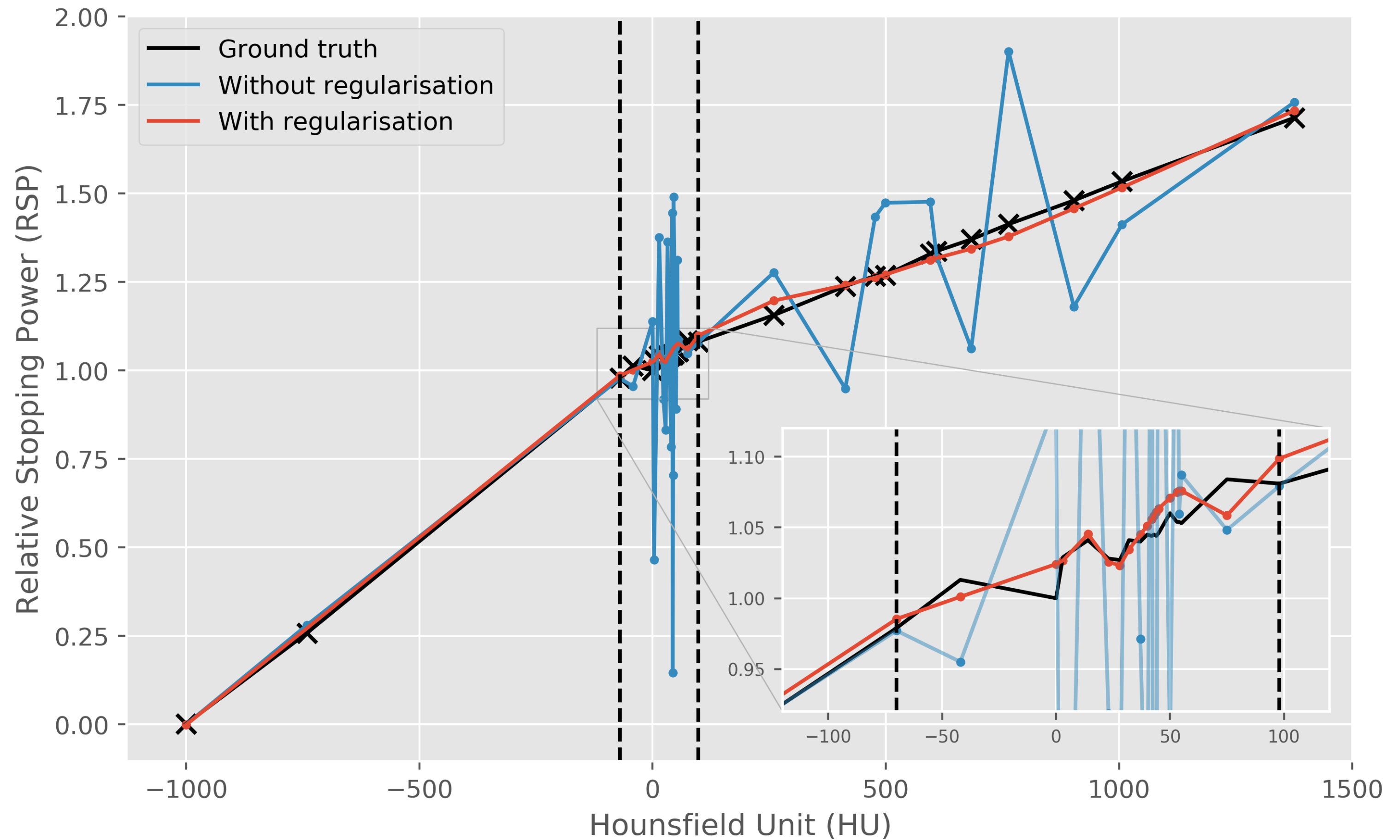
# Naïve optimization

Cost function contains only data term:

$$E_{\text{data}}(\vec{R}) = \|\vec{P} - A\vec{R}\|^2$$

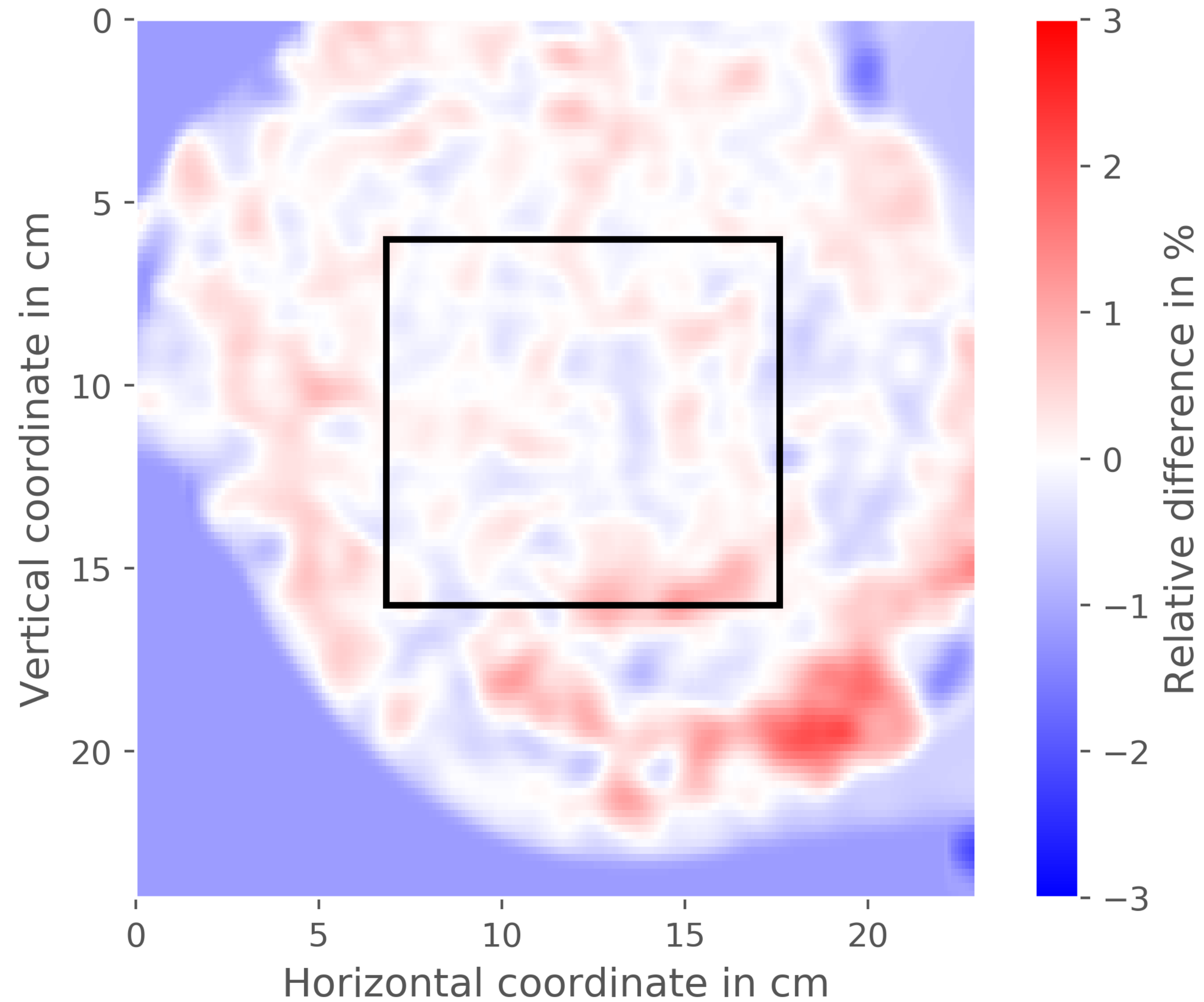
Find:

$$\hat{\vec{R}} = \operatorname{argmin} \left\{ E(\vec{R}) \right\}$$





# Residuals after optimization

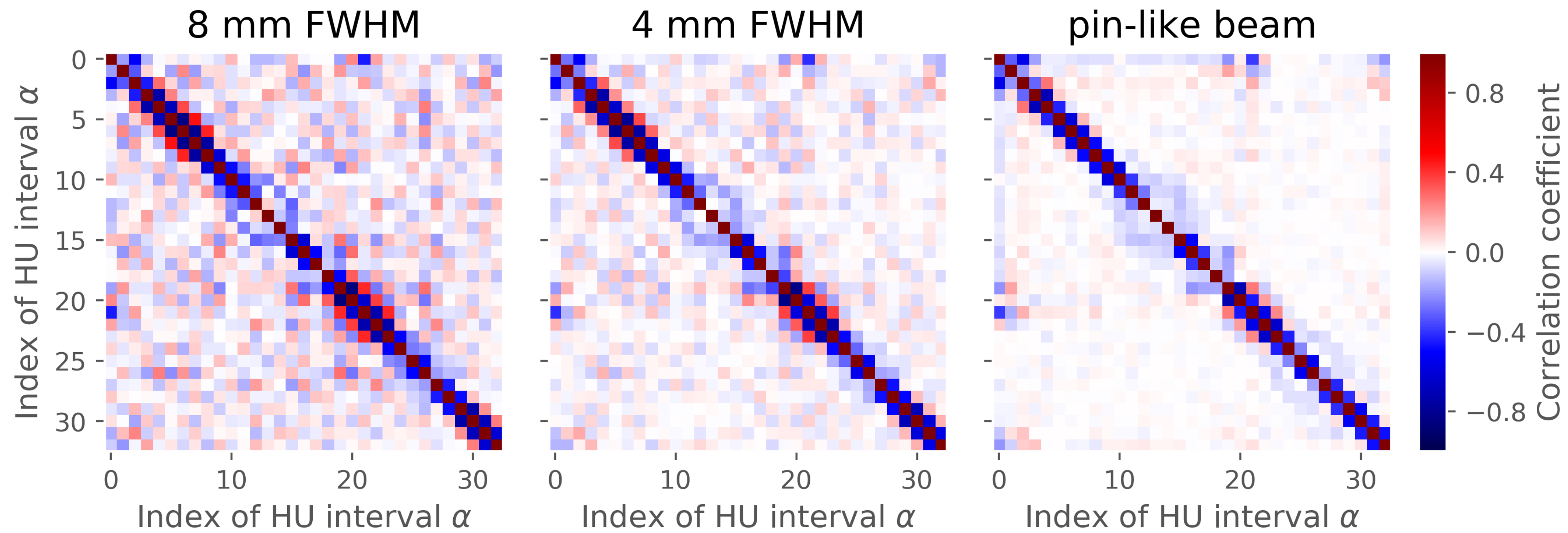


**What goes wrong?**

# Parameter correlation

Correlation coefficient:

$$\rho_{\alpha\alpha'} = \frac{\text{Cov}_{\alpha\alpha'}}{\sqrt{\text{Cov}_{\alpha\alpha} \text{Cov}_{\alpha'\alpha'}}} \quad \text{with} \quad \text{Cov}_{\alpha\alpha'} = (A^T A)^{-1}_{\alpha\alpha'}$$



**Size of proton beam is crucial**

# Regularization

Penalize variation of conversion curve:

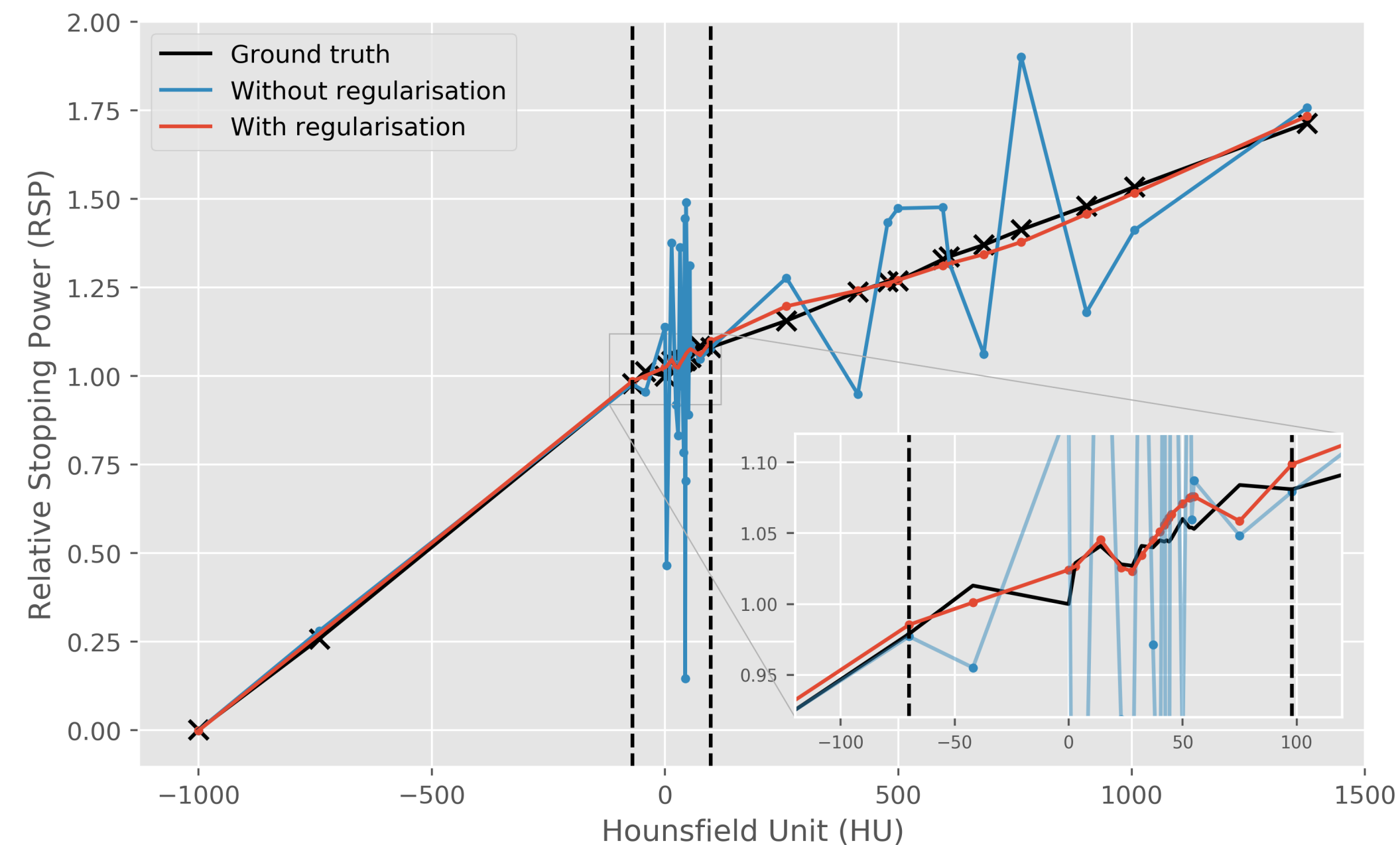
$$E_{\text{reg}} = \sum_{\alpha=\alpha_0}^{\alpha_M} (d_{\alpha+1} - d_{\alpha})^2 \quad \text{with} \quad d_{\alpha} = \frac{R_{\alpha} - R_{\alpha-1}}{H_{\alpha} - H_{\alpha-1}}$$

$$E(\vec{R}) = E_{\text{data}} + \gamma_{\text{air}} E_{\text{reg,air}} + \gamma_{\text{soft}} E_{\text{reg,soft}} + \gamma_{\text{bone}} E_{\text{reg,bone}}$$

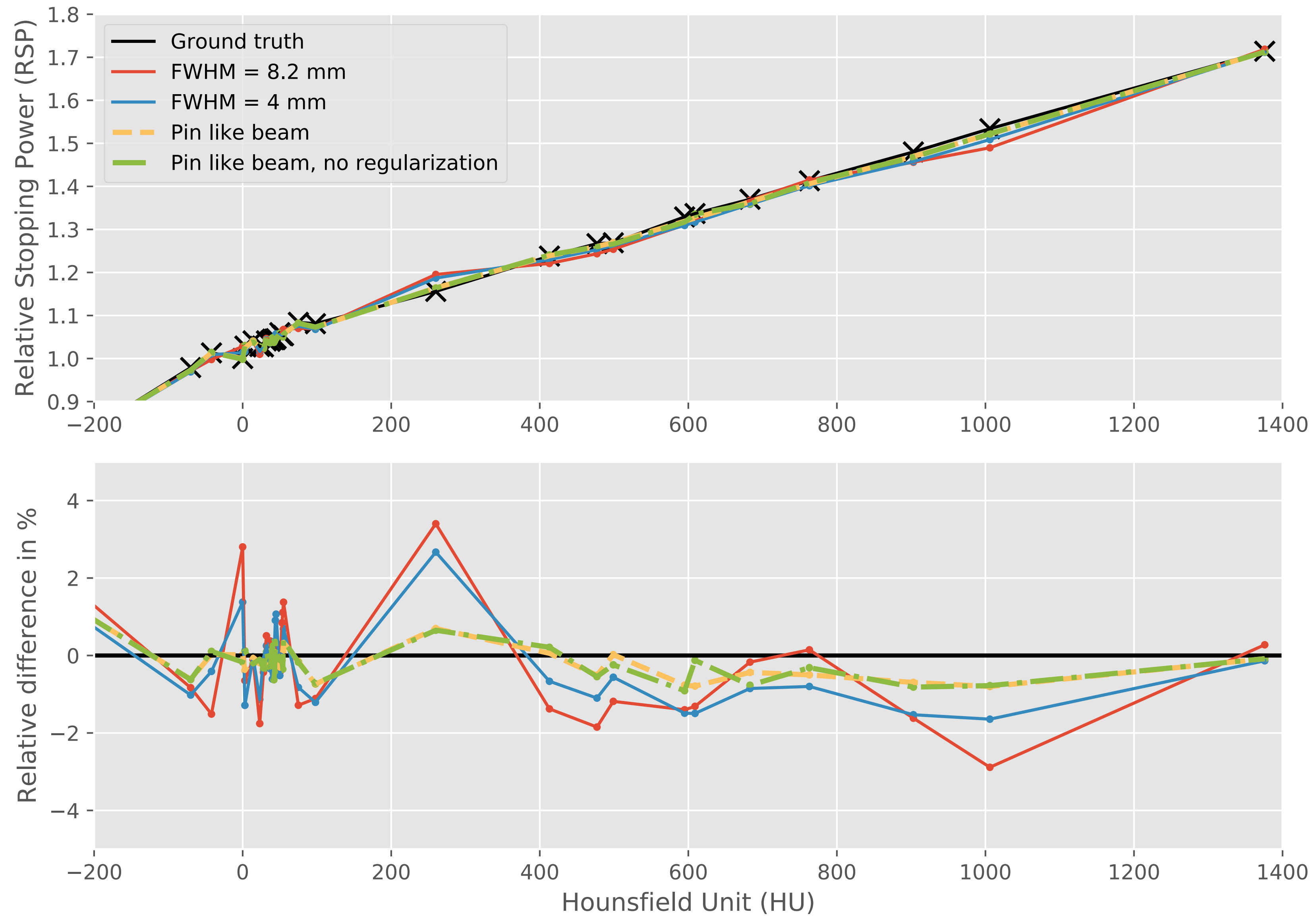
Note:  $E_{\text{reg}}$  can be written as matrix equation:

$$E_{\text{reg}} = \sum_{\alpha=\alpha_0}^{\alpha_M} (A_{\alpha'\alpha}^{\text{reg}} R_{\alpha})^2 = \|A^{\text{reg}} \vec{R}\|^2$$

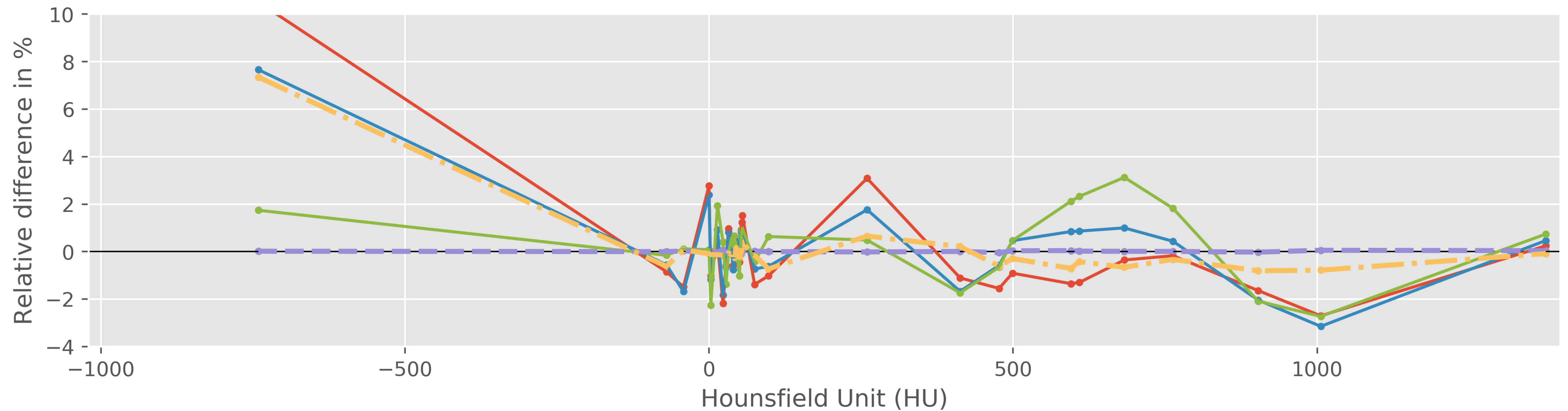
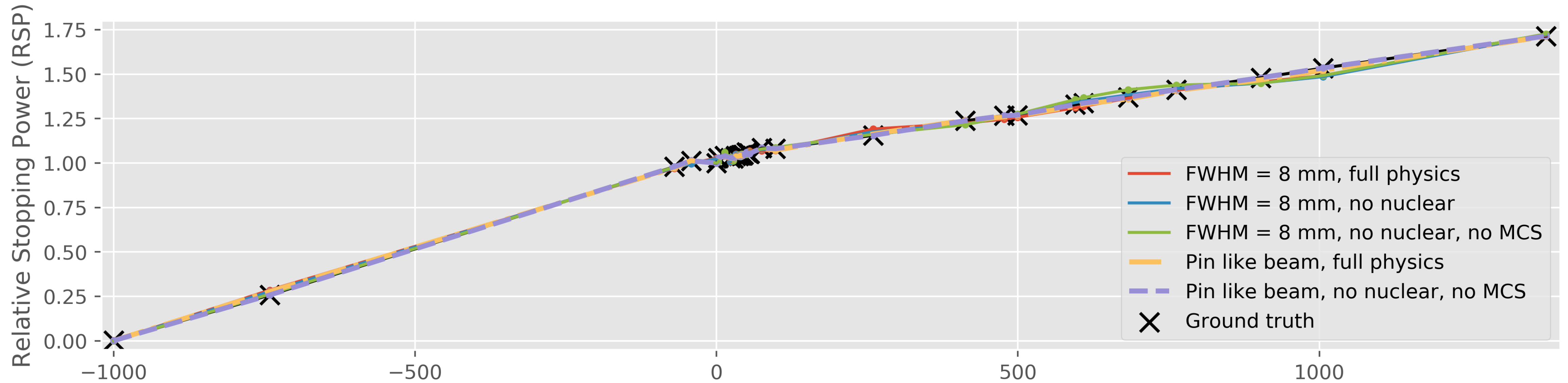
with  $A_{\alpha'\alpha}^{\text{reg}} = \frac{1}{H_{\alpha+1} - H_{\alpha-1}} (\delta_{\alpha',\alpha-1} - 2\delta_{\alpha',\alpha} + \delta_{\alpha',\alpha+1})$ , with  $\delta_{\alpha',\alpha} = \begin{cases} 1 & \text{for } \alpha' = \alpha \\ 0 & \text{otherwise.} \end{cases}$



# Regularization: proton beam size matters



# Regularization: does physics matter?



# How to choose the regularization weights?

$$E(\vec{R}) = E_{\text{data}} + \gamma_{\text{air}} E_{\text{reg,air}} + \gamma_{\text{soft}} E_{\text{reg,soft}} + \gamma_{\text{bone}} E_{\text{reg,bone}}$$

Choose the weighting factors so that the regularizer cost of the optimized curve is similar to that of a reference curve. (by iteration)

Less variation expected -> higher weight

More variation expected -> lower weight

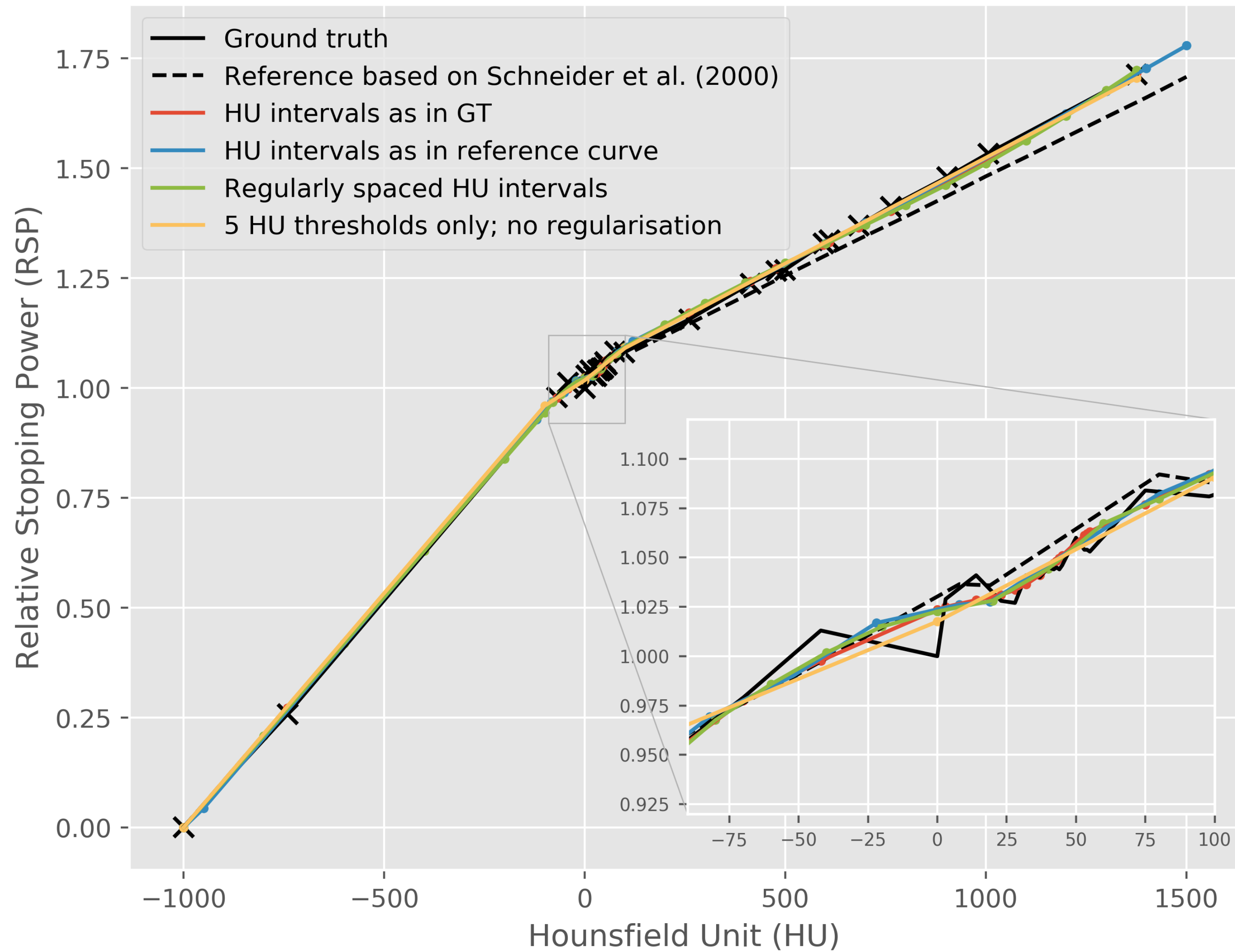
# Choose regularizer weights based on reference curve



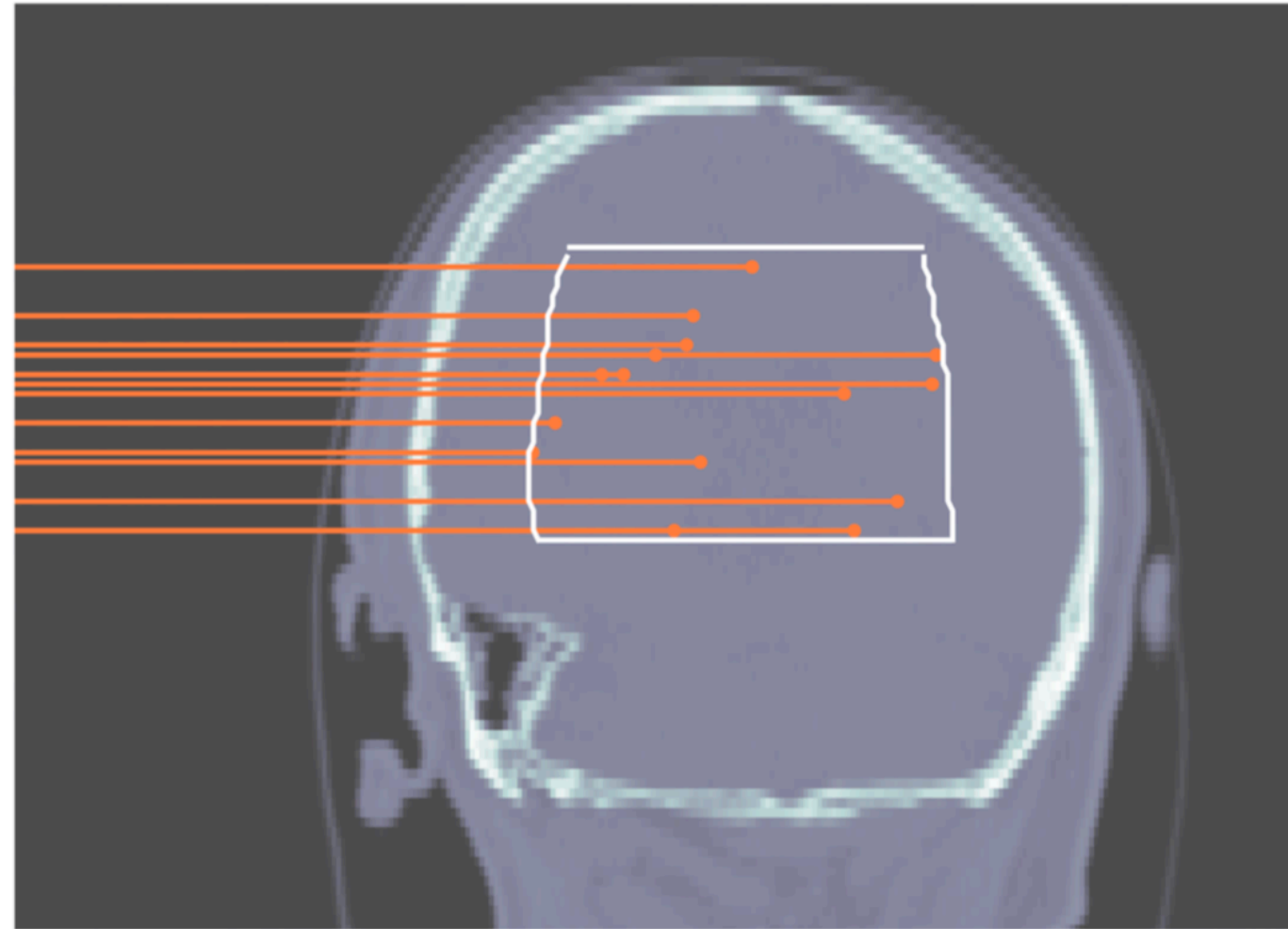


**And what about the CT number intervals?**

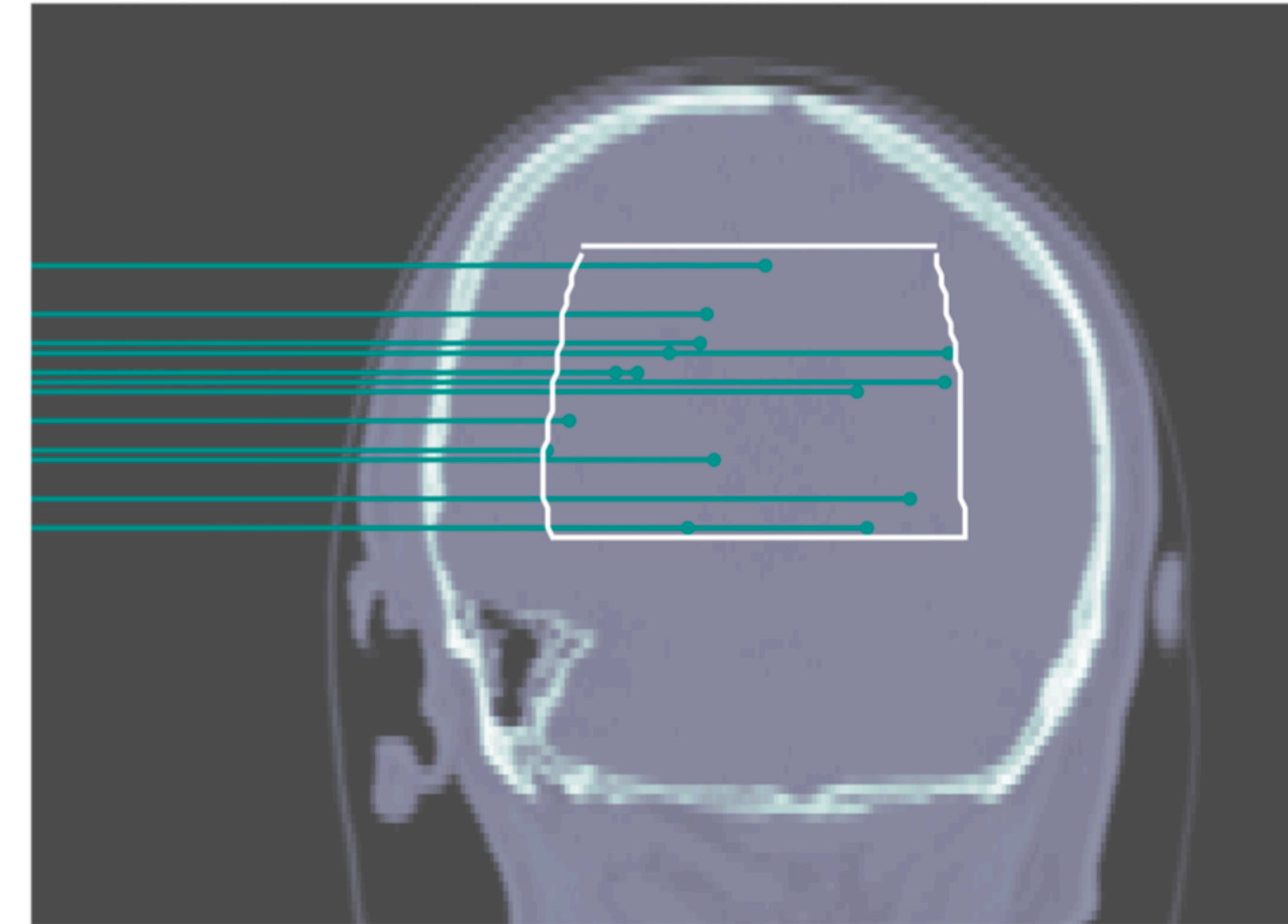
# And what about the CT number intervals?



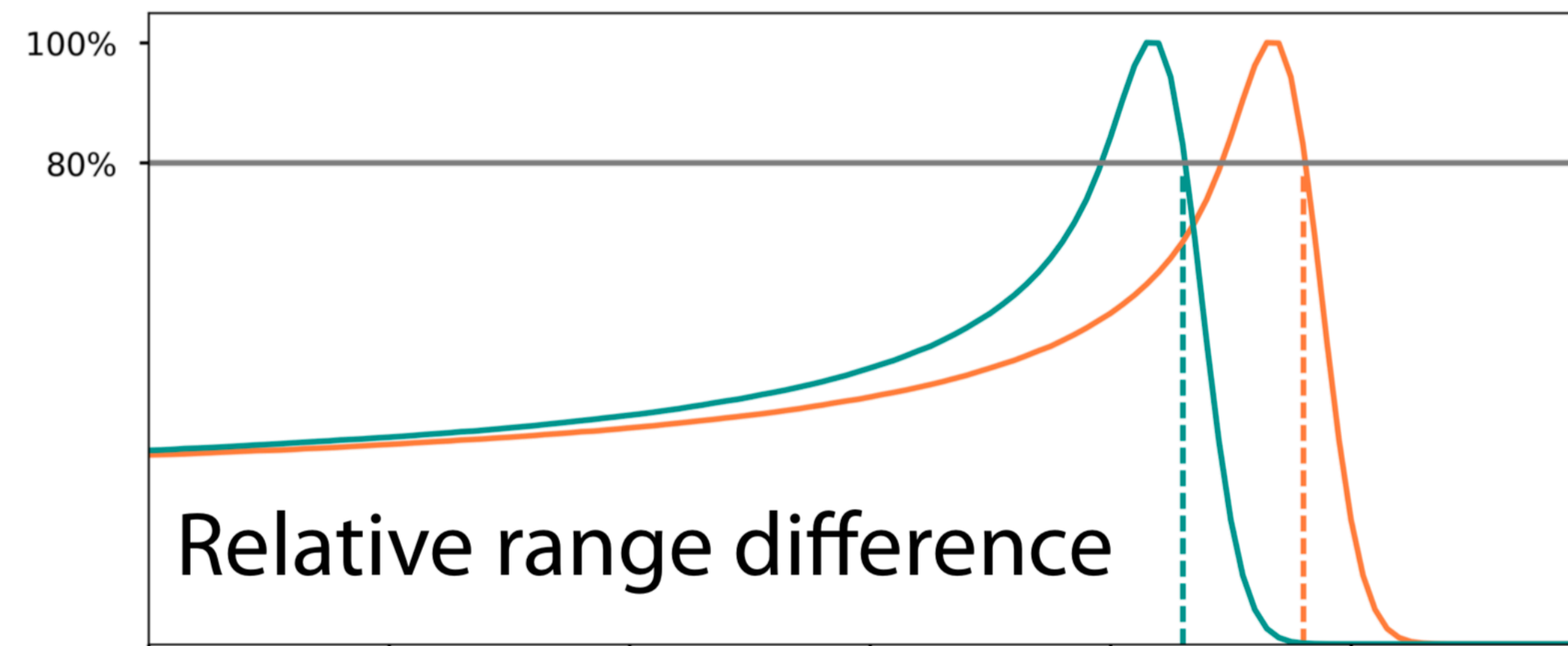
# Test range accuracy in Monte Carlo simulation



with GT HU-RSP curve

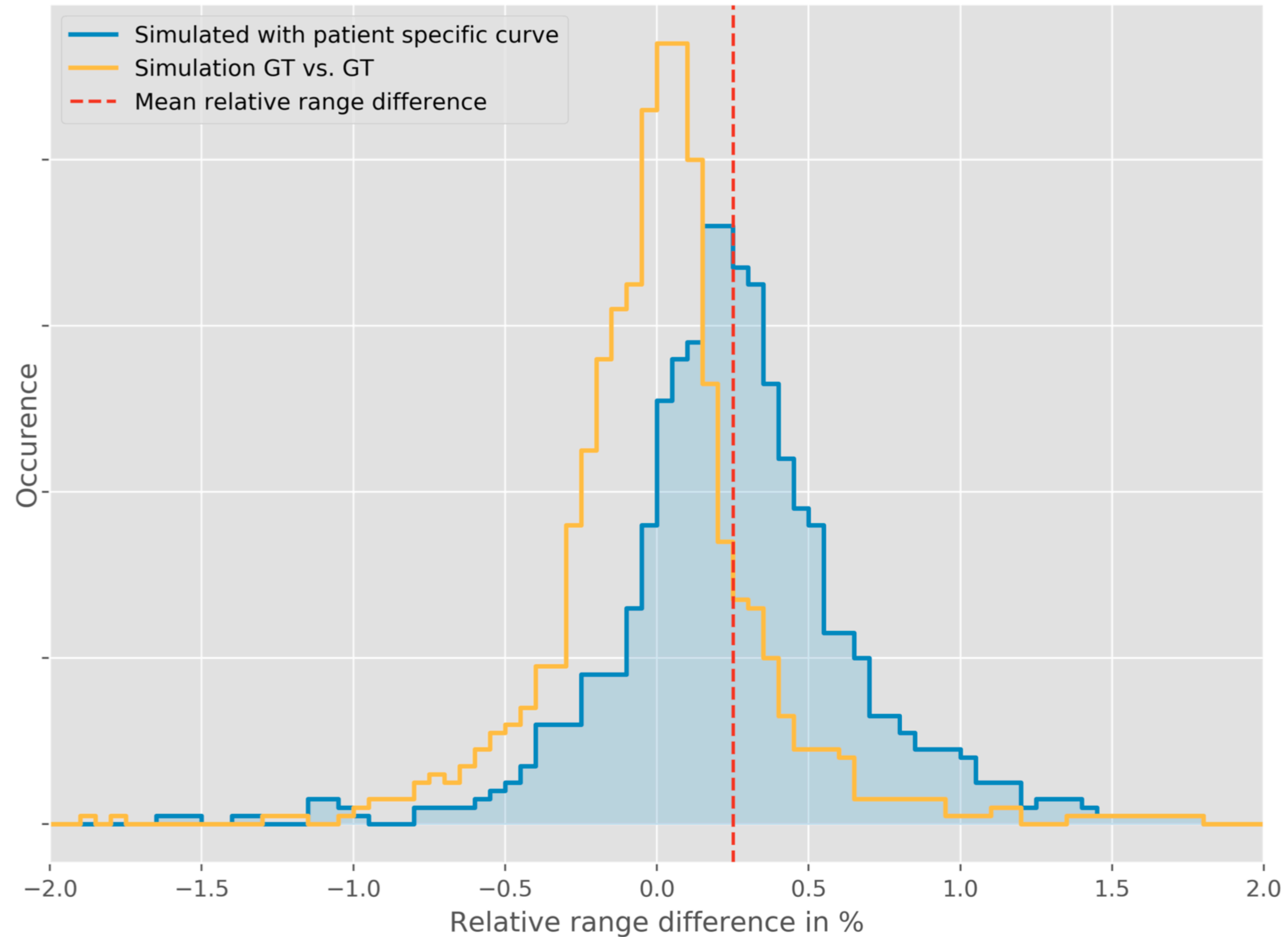


with re-calibrated curves



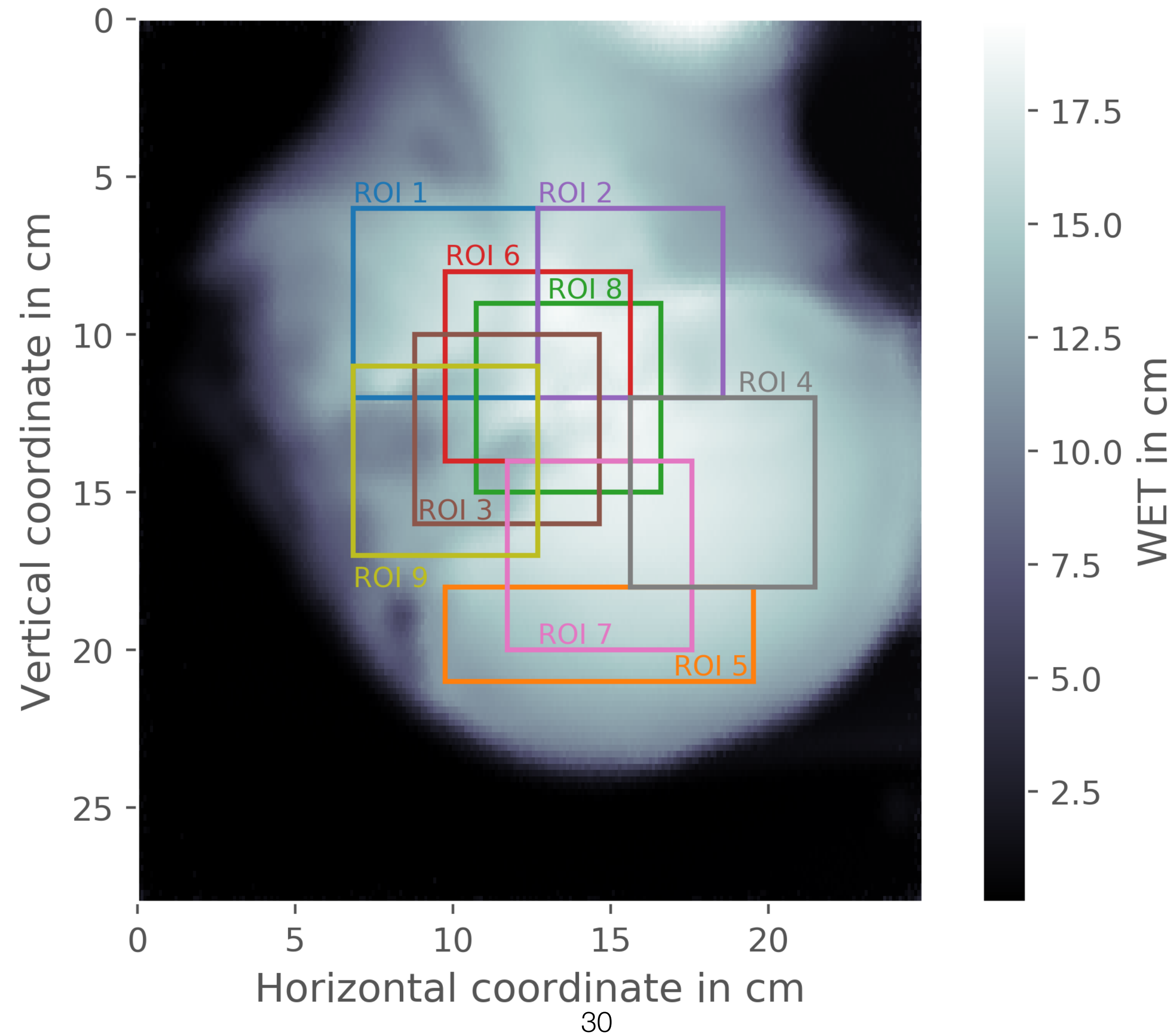
- 1000 PB
- Random position
- Random energy

# Range accuracy with optimized CT-RSP curve

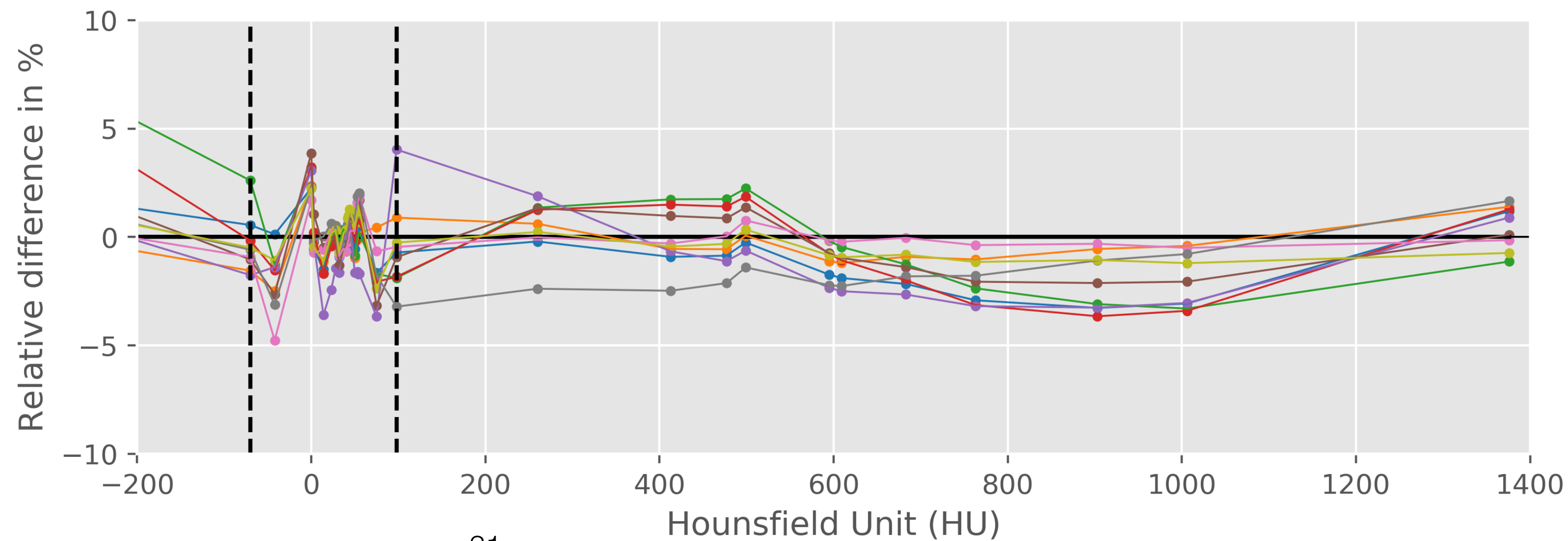
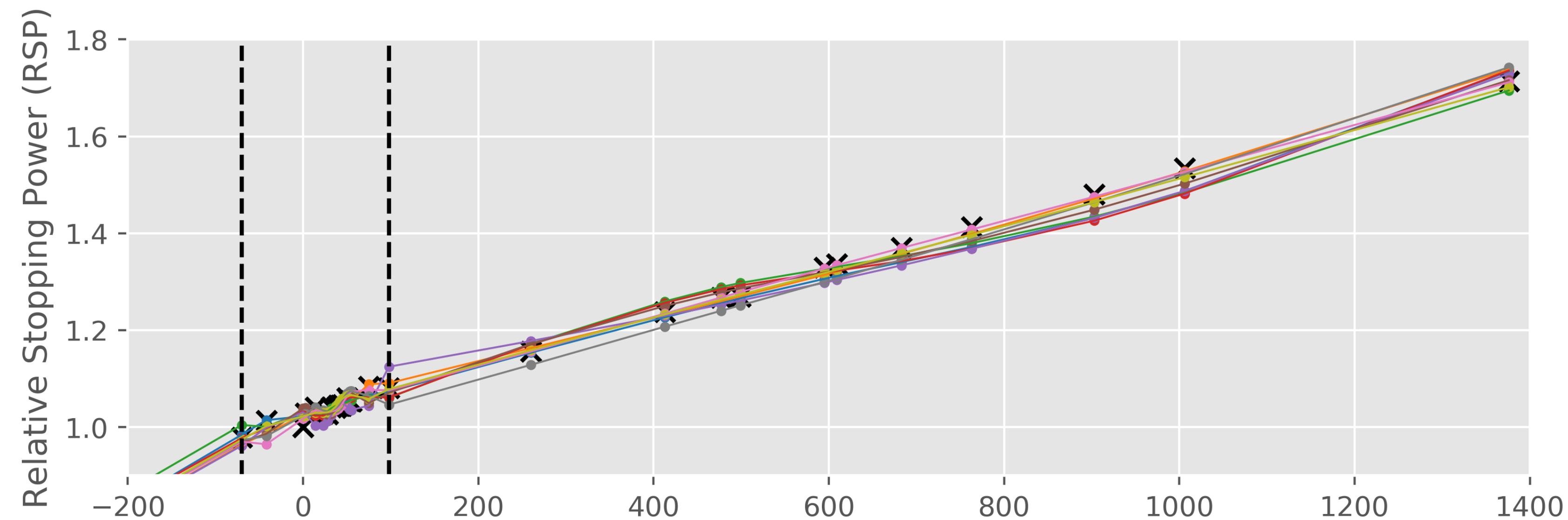
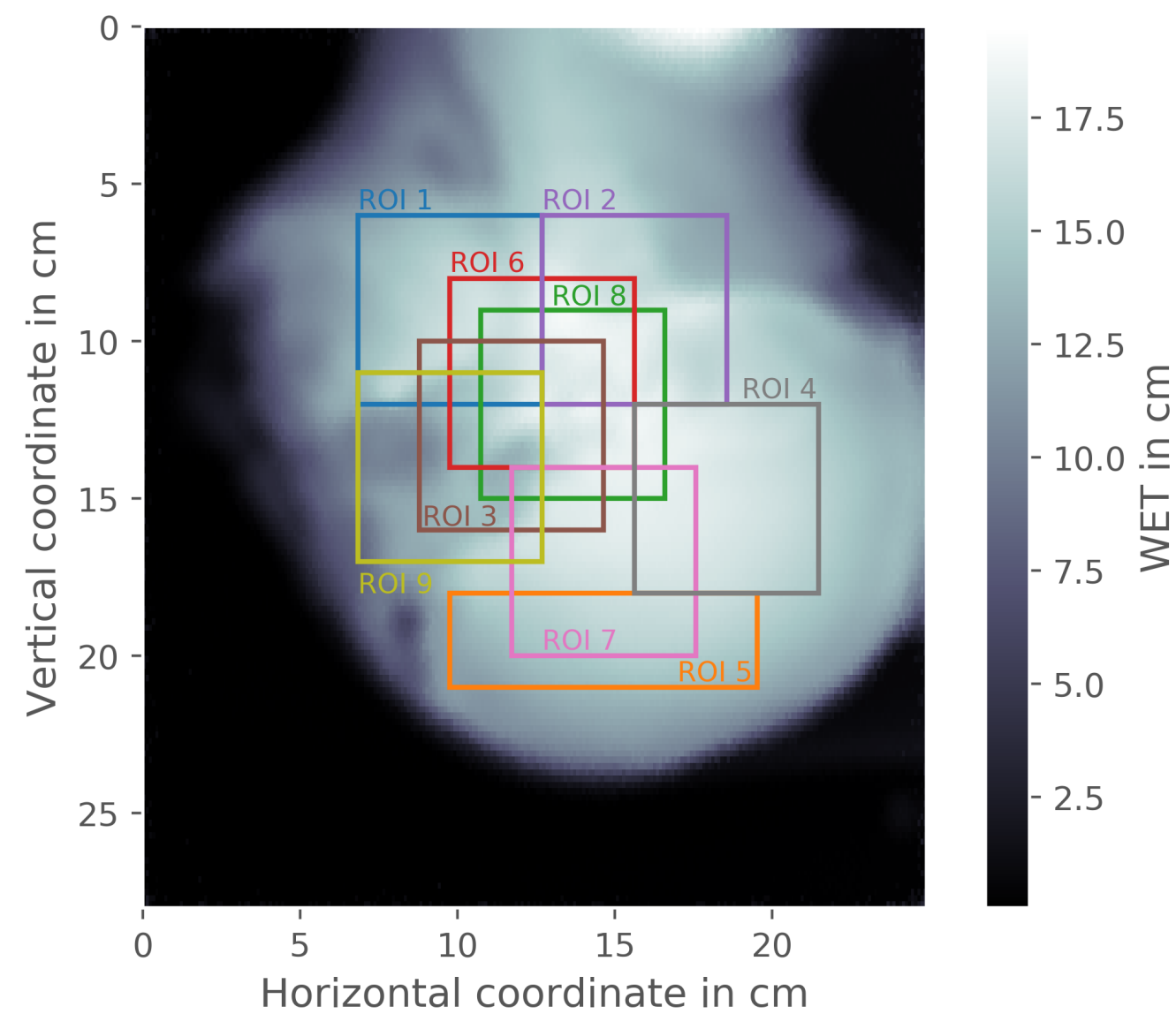


**Does it matter of which region in the patient  
the proton radiography is acquired?**

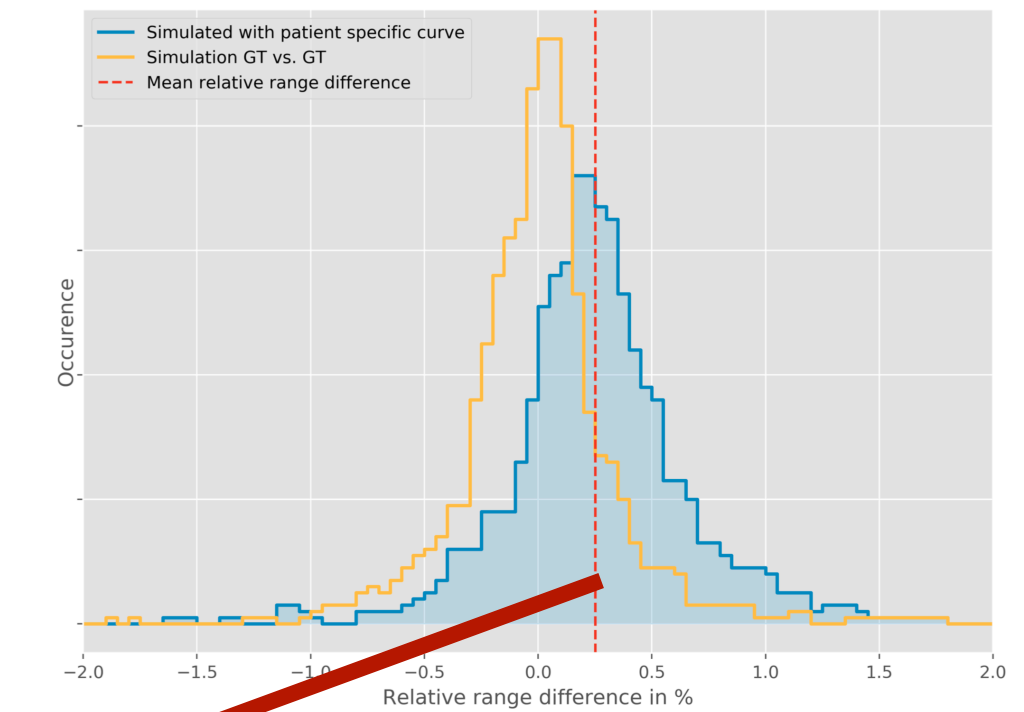
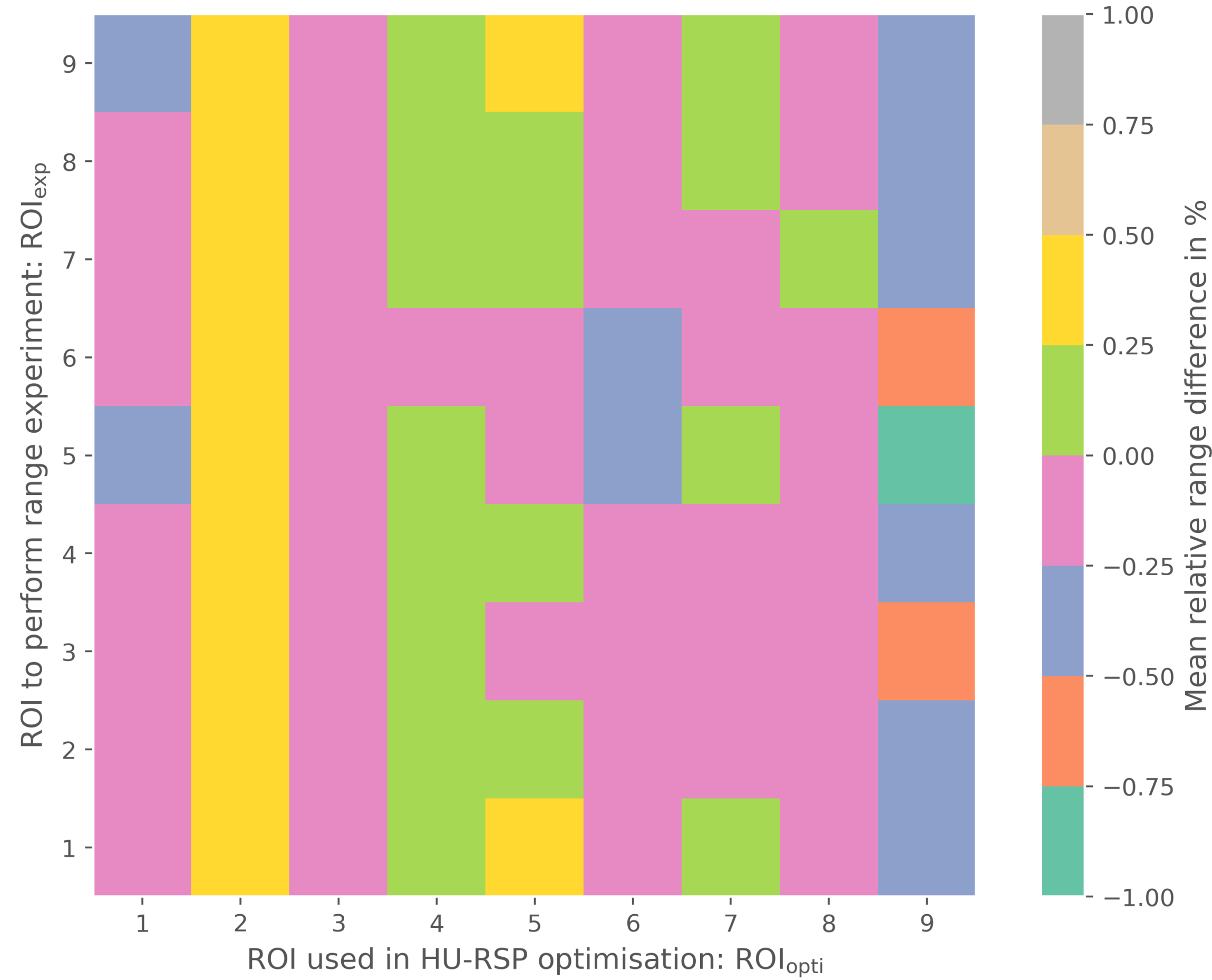
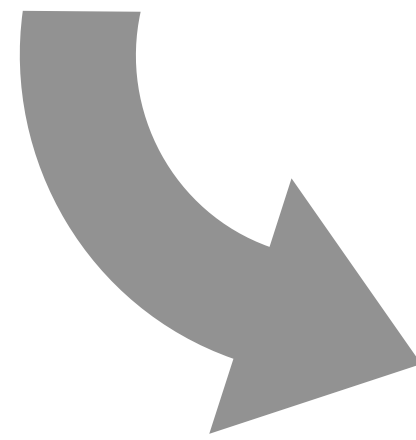
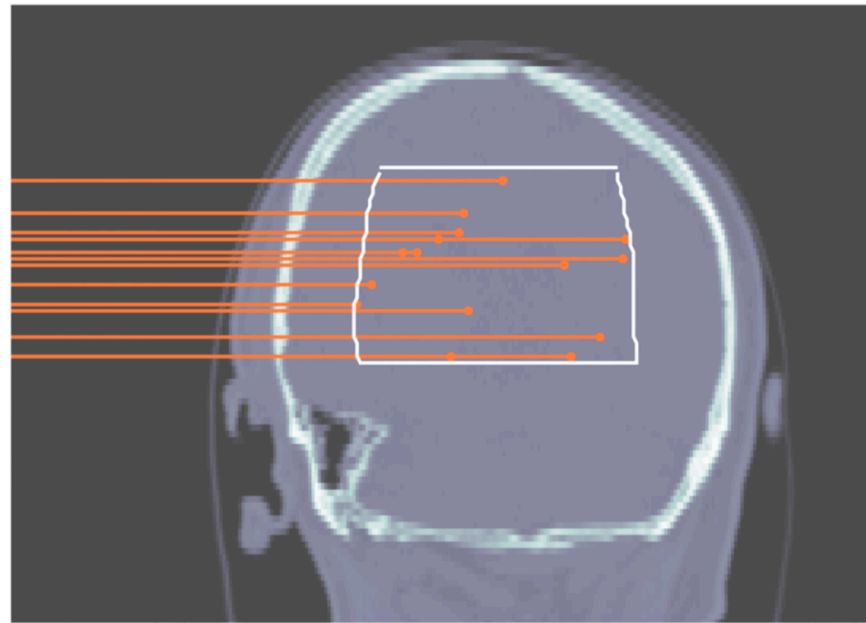
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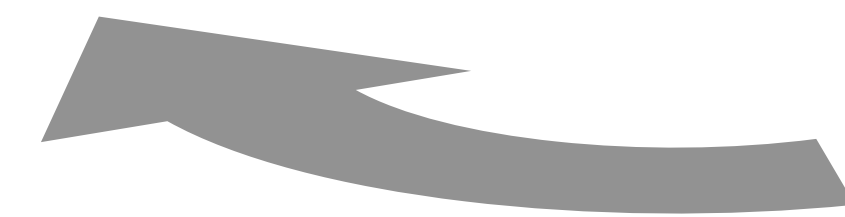
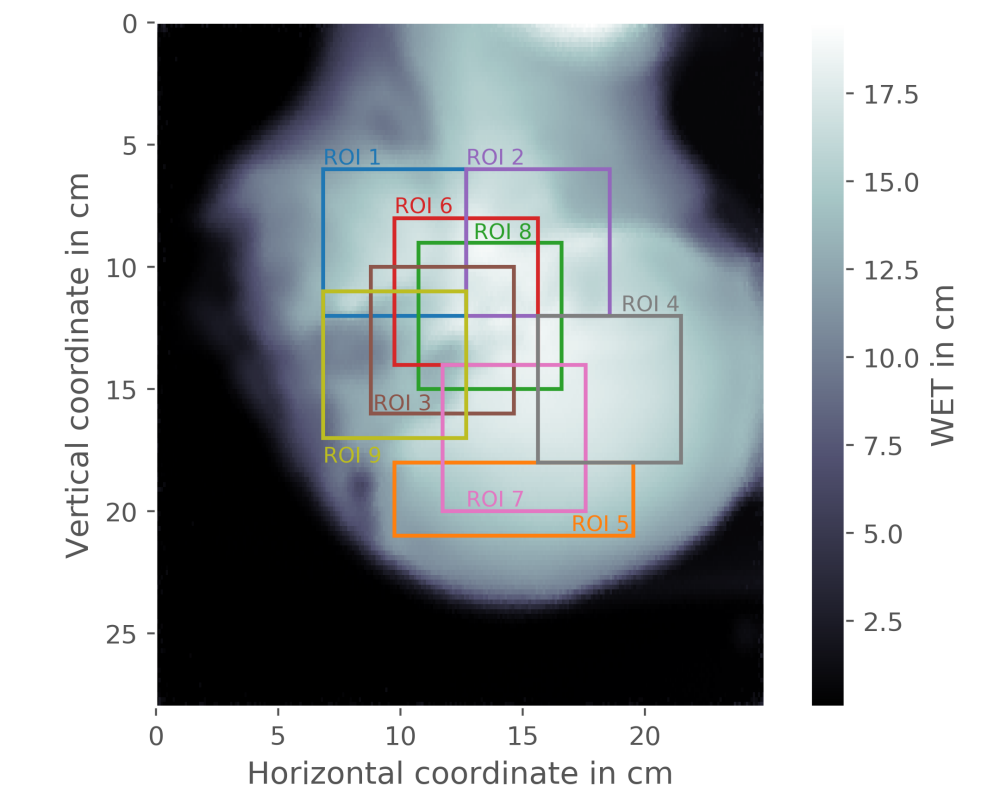
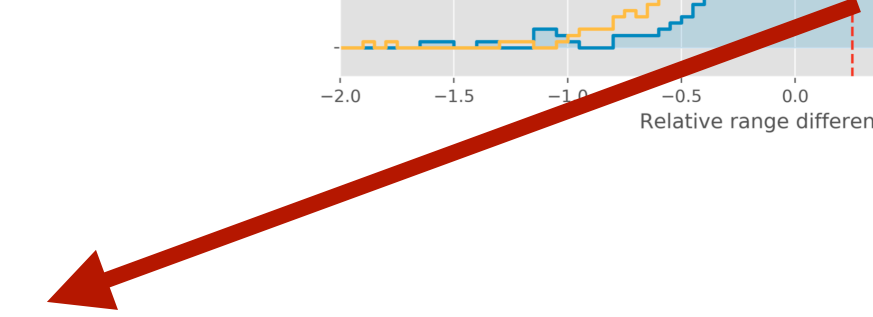
# Does it matter of which region in the patient the proton radiography is acquired?



# Does it matter of which region in the patient the proton radiography is acquired?



Mean relative range difference in %

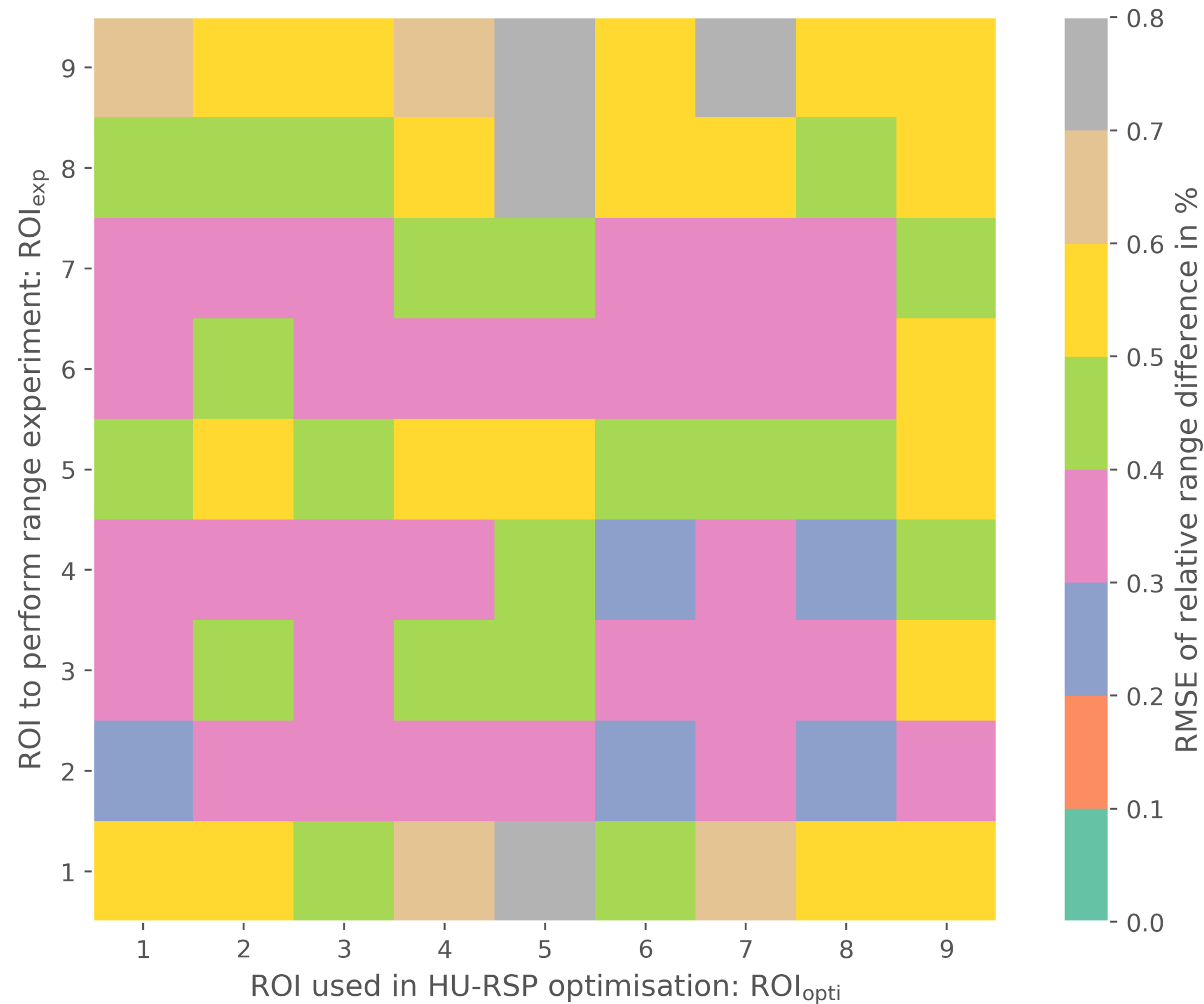




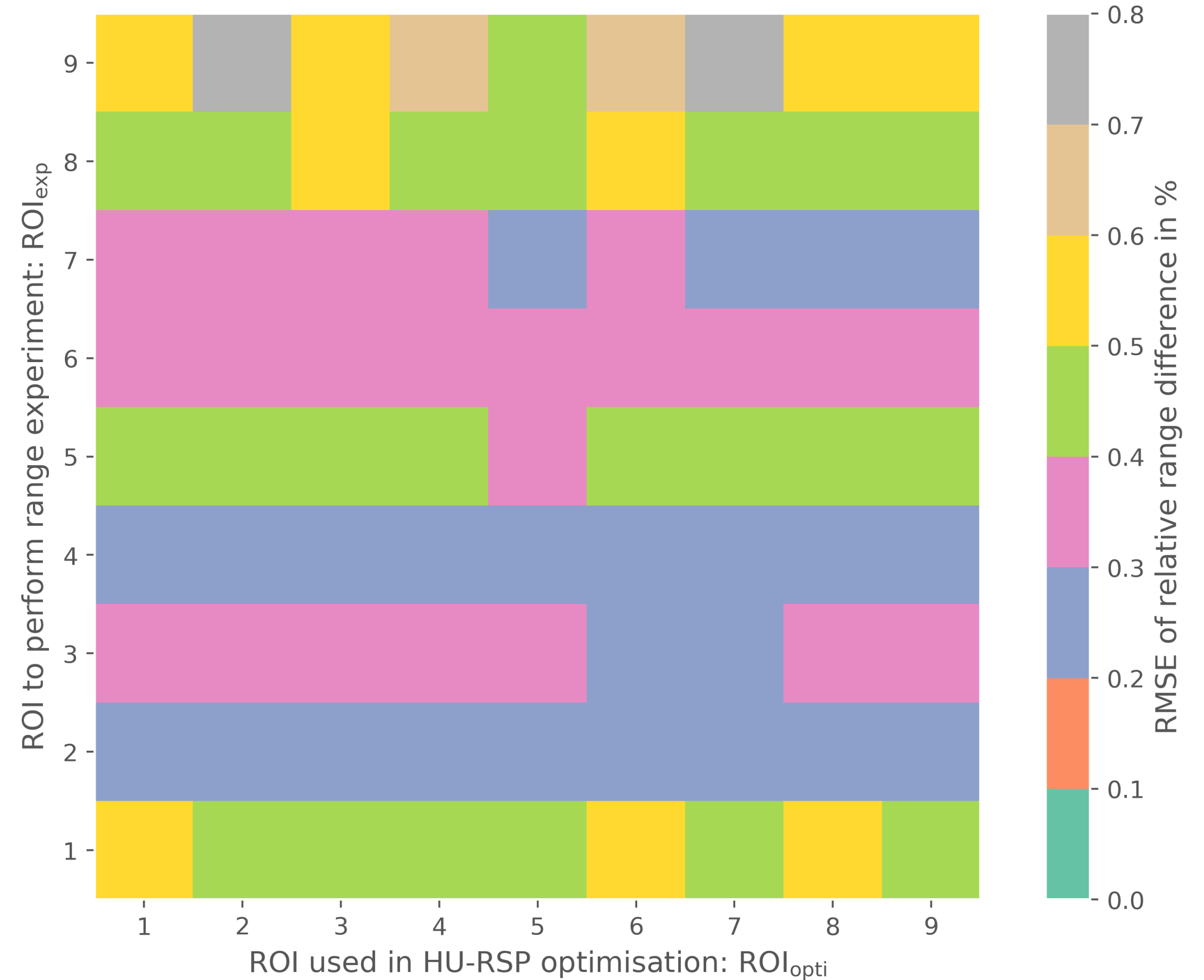
# Does it matter of which region in the patient the proton radiography is acquired?

## Standard deviation of range distribution

### Optimized vs. ground truth



### Ground truth vs. ground truth



# Summary

- **Patient specific calibration of CT-RSP curve feasible with relatively simple imaging system.**
- **Optimization needs to be regularized.**
- **Range accuracy with optimized curve better than 0.5%**
- **Region of which the proton radiography is acquired is not essential**
- **Intra-patient tissue variability not considered by this study**
- **Poor one-to-one correspondence between CT number & RSP cannot be resolved by patient specific conversion**

**Thank you**

