



Northern Illinois University

Optimizing relaxation parameter for iterative pCT reconstructions

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July 20, 2020

Proton CT



- Proton CT measures the RSP of each voxel directly
- This allows for reduction of beam-specific range margins during treatment planning
- This could lead to a reduction of NTCP on structures close to the CTV



- Single particle tracking
- 1 MHz protons
- 10 x 30 cm field of view
- 6 minute, continuous rotation scans
- 360 million protons
- About 100 million protons after preprocessing

Image Reconstruction



- Most likely path (MLP) algorithm
- Feldkamp, Davis, Kress (FDK) cone beam filtered back projection for initial image reconstruction
- Component Averaged Row Projection (CARP)
 - String average projection (SAP) iterative algorithm
- Total variation superiorization (TVS)
- Reconstruction on cluster with GPUs and CPUs
 - Allows for large amounts of parallelization and faster reconstruction times

pCT Iterative Reconstruction – CARP



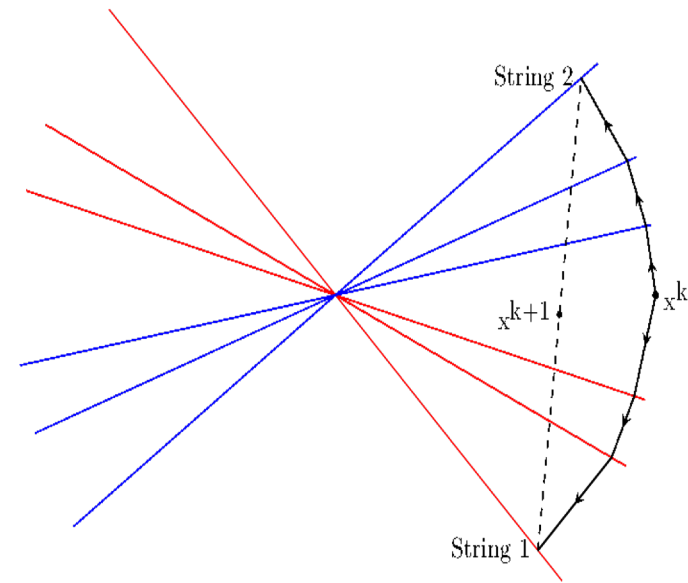
$$\bullet Ax = b, A = \begin{bmatrix} \square & \square & \square \\ \leftarrow & a^i & \rightarrow \\ \square & \square & \square \\ \square & \square & \square \\ \square & \square & \square \end{bmatrix}, x = \begin{bmatrix} \square \\ \square \\ \square \end{bmatrix}, b = \begin{bmatrix} \square \\ b_i \\ \square \\ \square \\ \square \end{bmatrix}$$

$$x^{(k+1)} = \frac{1}{s} \sum_{t=1}^M S_t(x^{(k)})$$

$$S_t(x^{(k)}) = x^{(k)} + \lambda \sum_i \frac{b_i - \langle a^i, x^{(k)} \rangle}{\|a^i\|^2} a^i$$

a^i = proton path length per voxel
 x = RSP in each voxel
 b = WEPL per proton track

i = index for proton track
 $\frac{1}{s}$ = weighting factor
 λ = relaxation parameter



k = iteration number
 M = total number of strings = 40
 t = String number, {1...40}

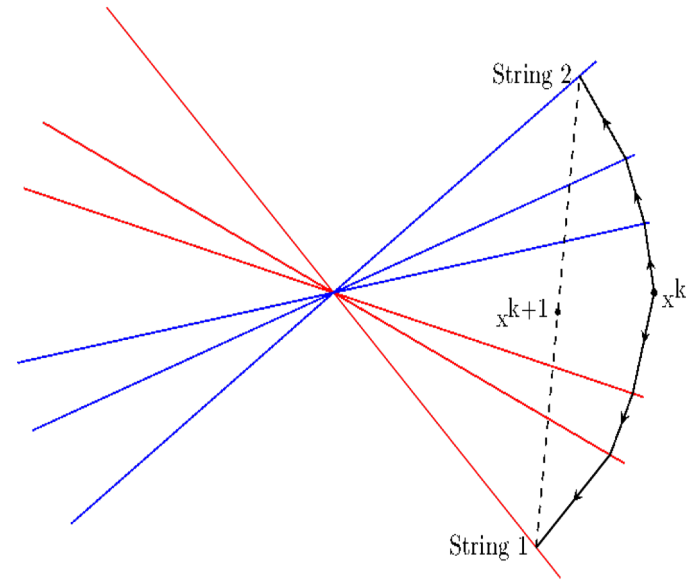
pCT Iterative Reconstruction – CARP



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Goal

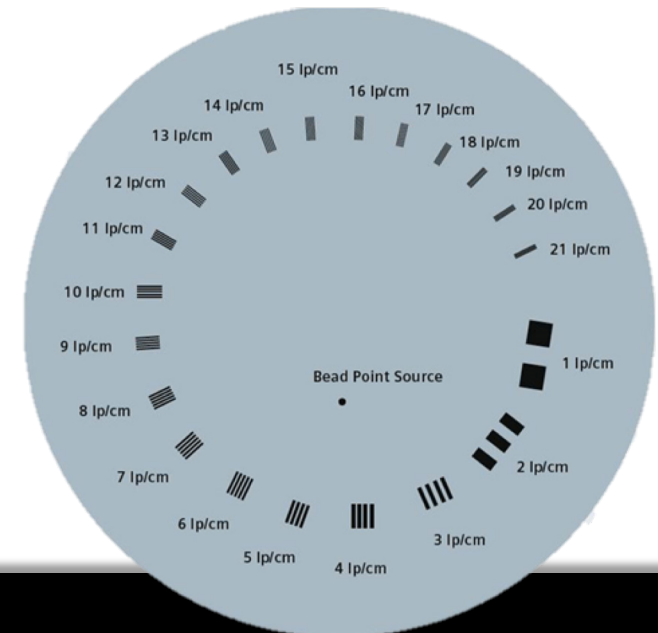


- Vary relaxation parameter in CARP algorithm and observe changes in image quality metrics
- Observe how the image quality metrics evolve with iteration number
- Image quality metrics:
 - RSP Accuracy
 - Contrast to Noise Ratio (CNR)
 - $CNR = \frac{RSP_A - RSP_B}{\sqrt{(\sigma_A)^2 + (\sigma_B)^2}}$, where σ is the standard deviation in the RSP
 - Spatial resolution / Modulation transfer function (MTF)
 - $MTF(LP) = \frac{(Peak - Valley)_{LP}}{(Peak - Valley)_{LP=1 \text{ cm}^{-1}}}$

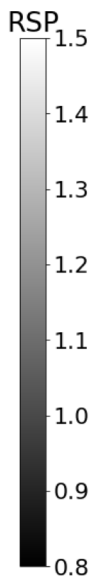
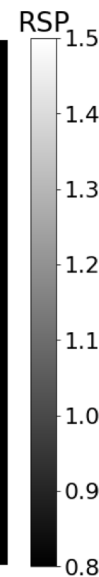
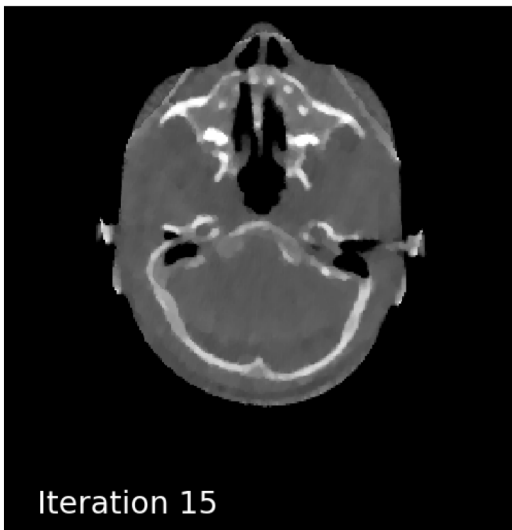
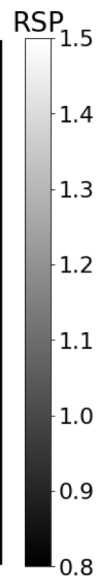
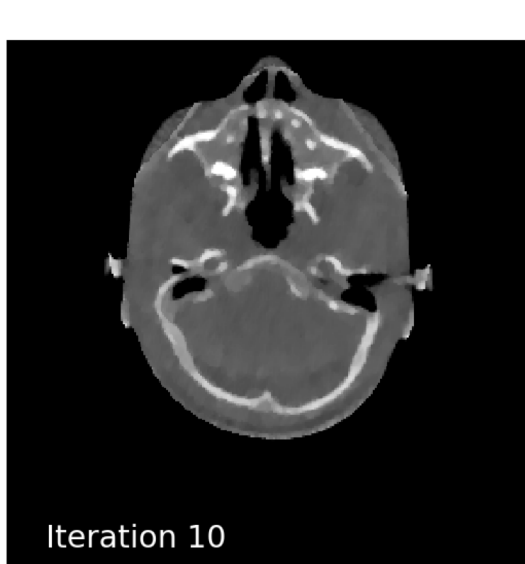
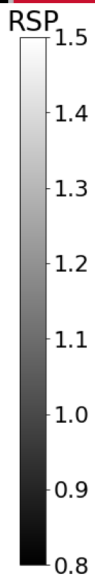
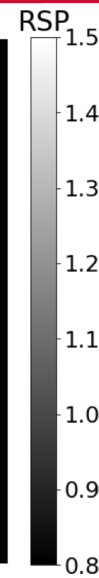
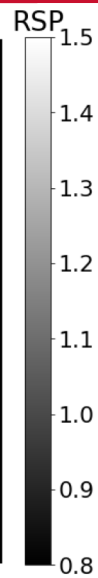
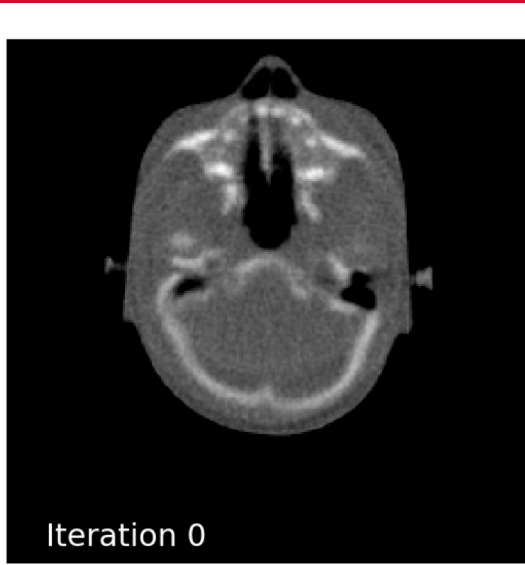
Phantoms



- Custom RSP phantom
- Line pair phantom
- CIRS pediatric head phantom



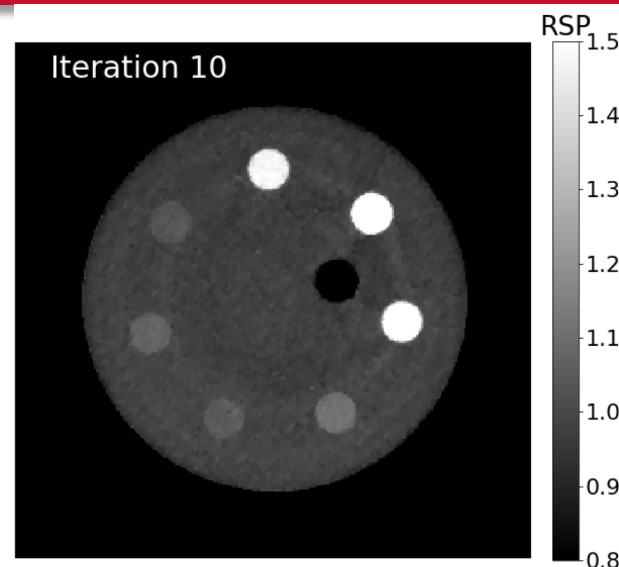
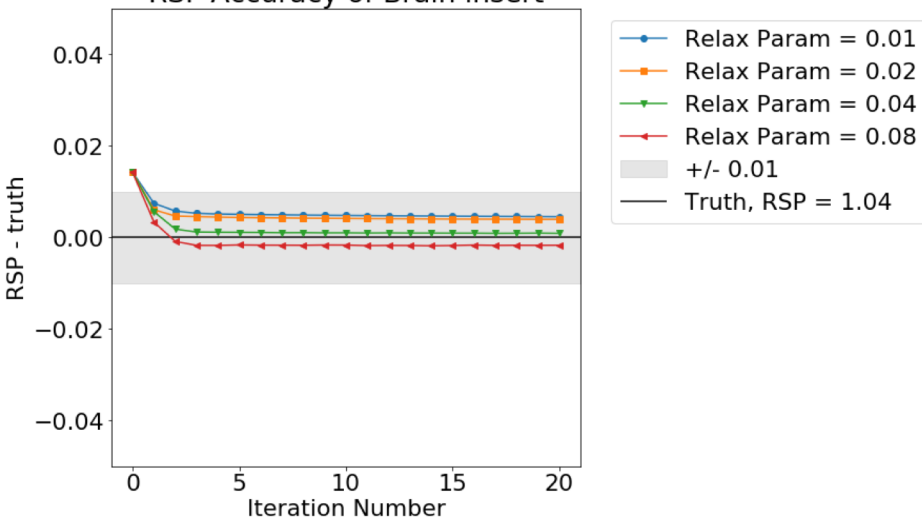
Reconstruction per iteration



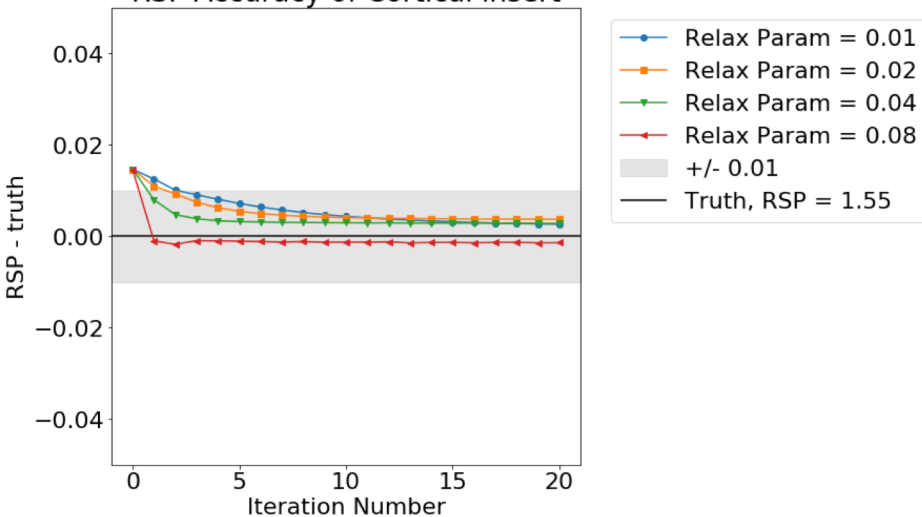
RSP Accuracy using custom RSP phantom (CIRS tissue substitutes)



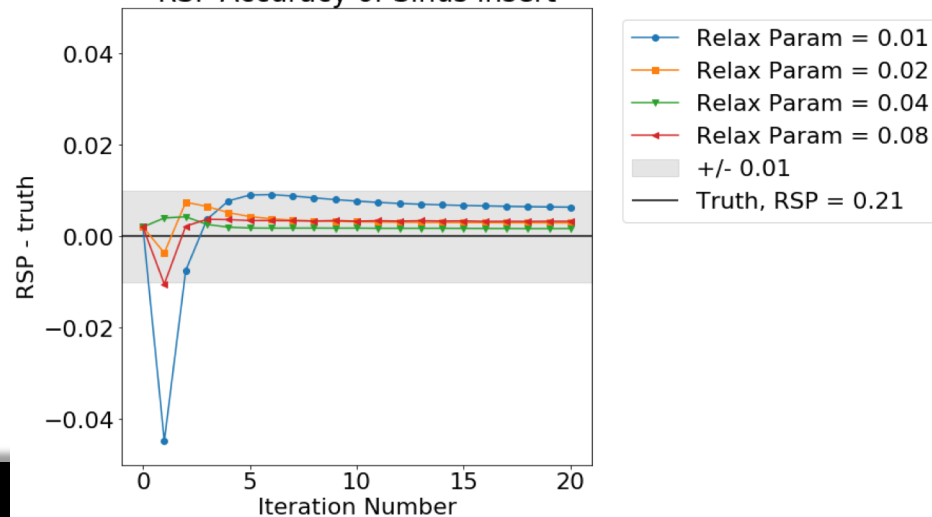
RSP Accuracy of Brain insert



RSP Accuracy of Cortical insert



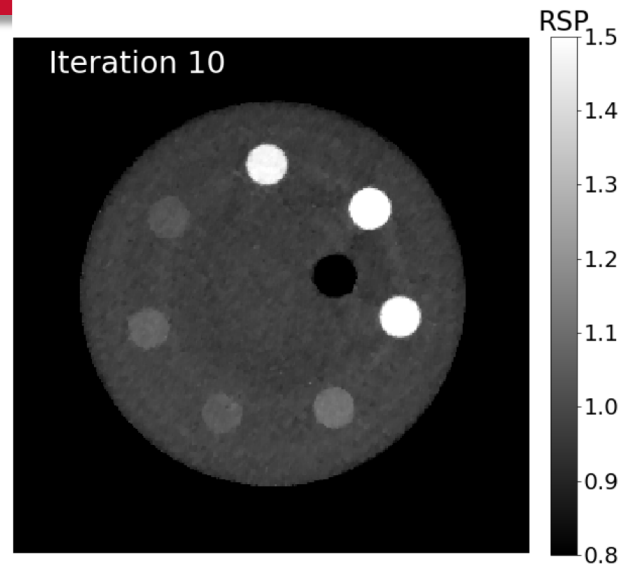
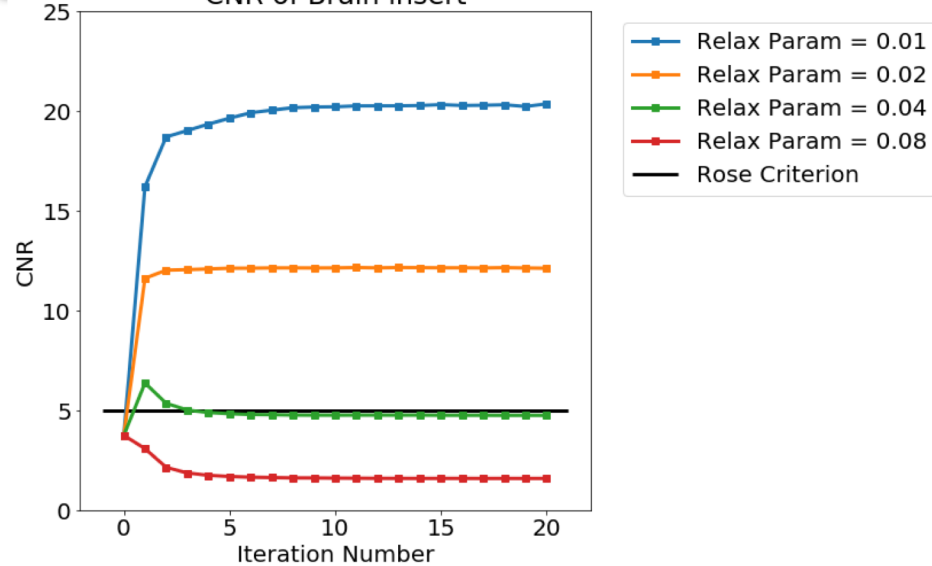
RSP Accuracy of Sinus insert



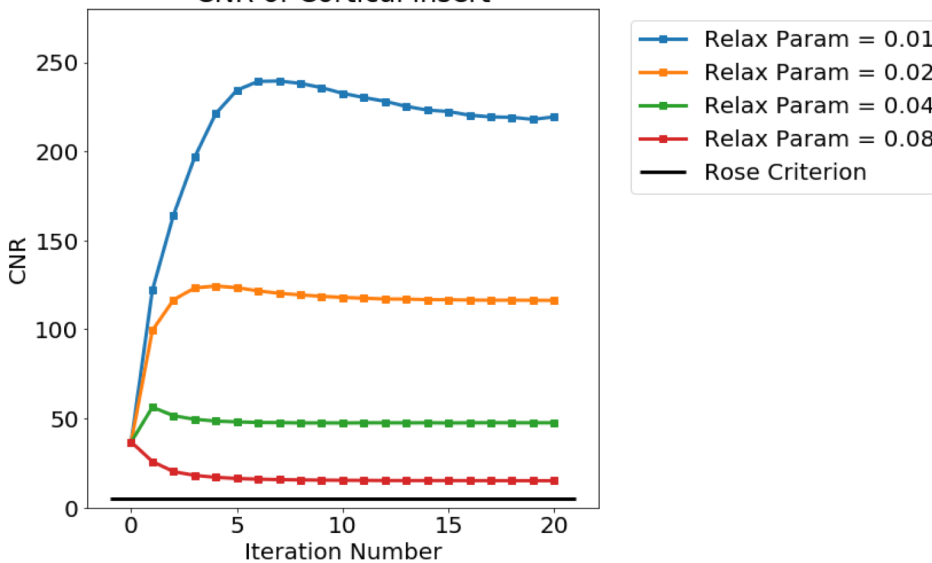
Contrast-to-Noise Ratio (CNR) using custom RSP phantom



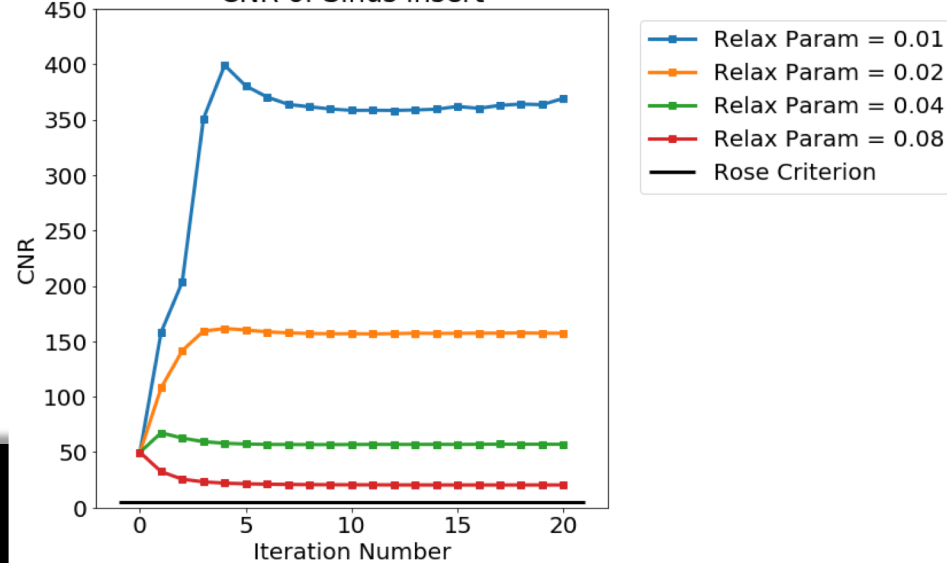
CNR of Brain insert



CNR of Cortical insert



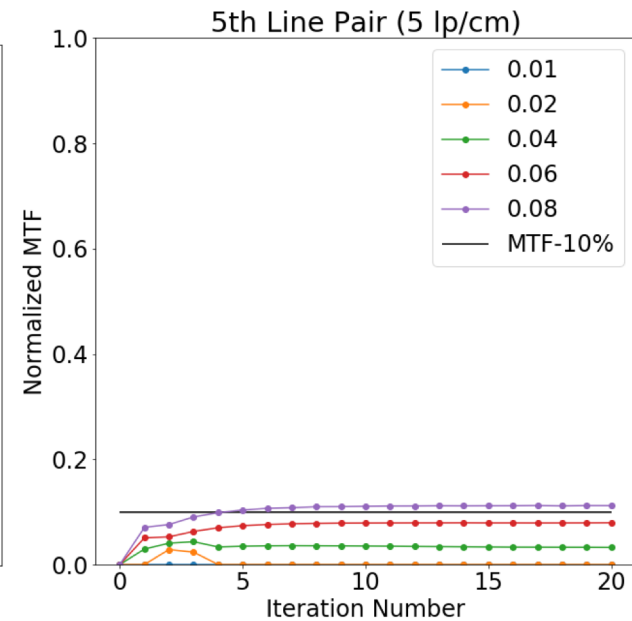
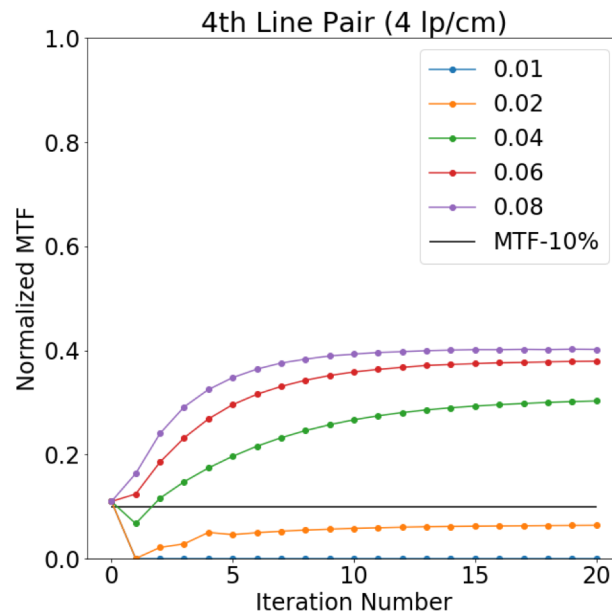
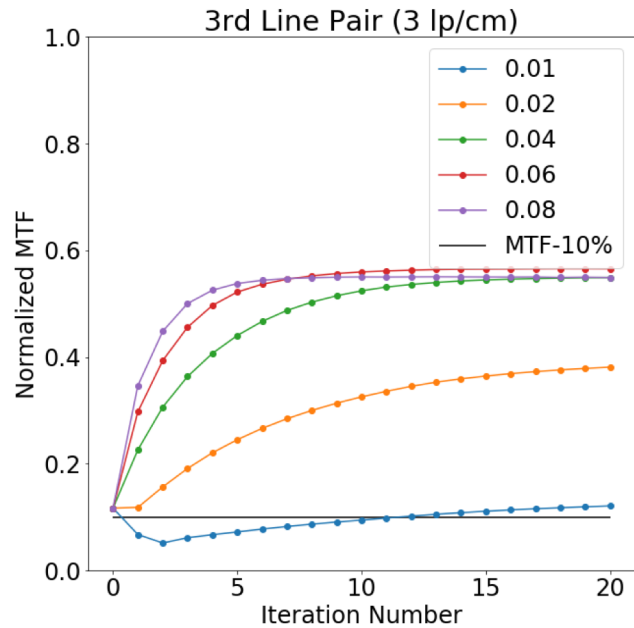
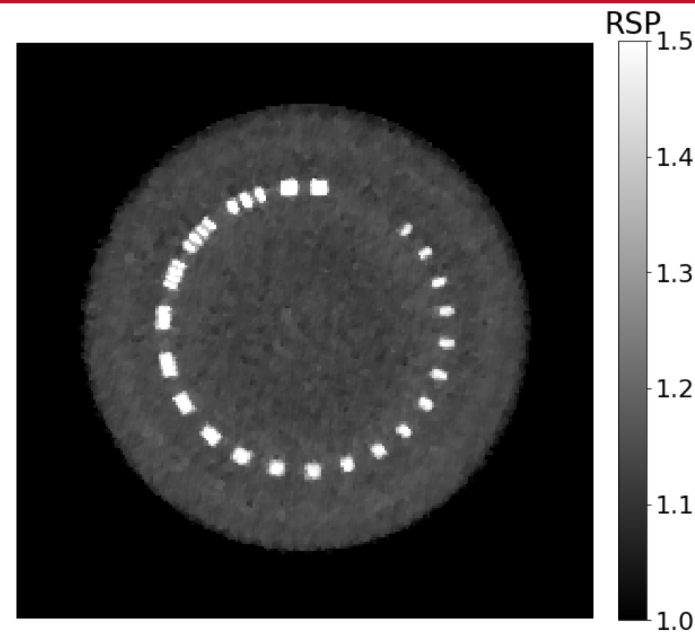
CNR of Sinus insert



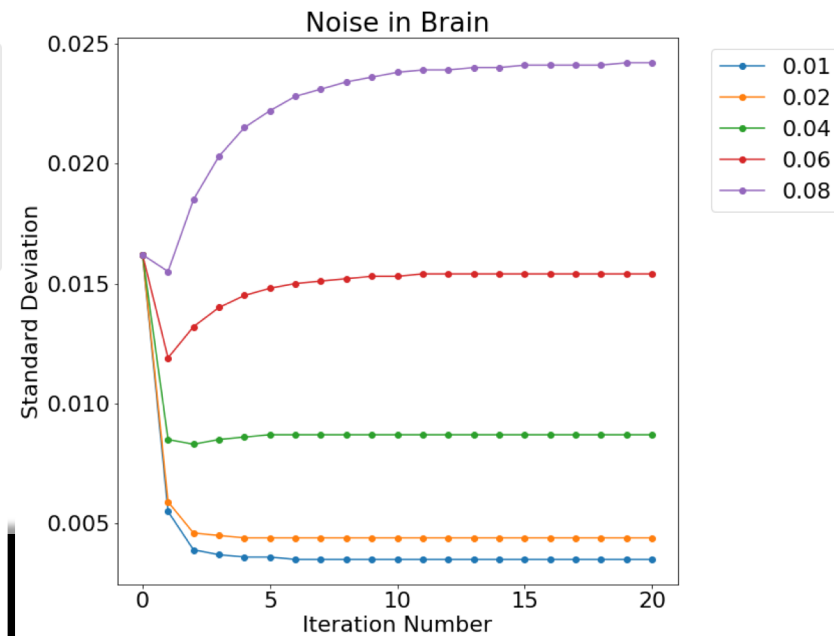
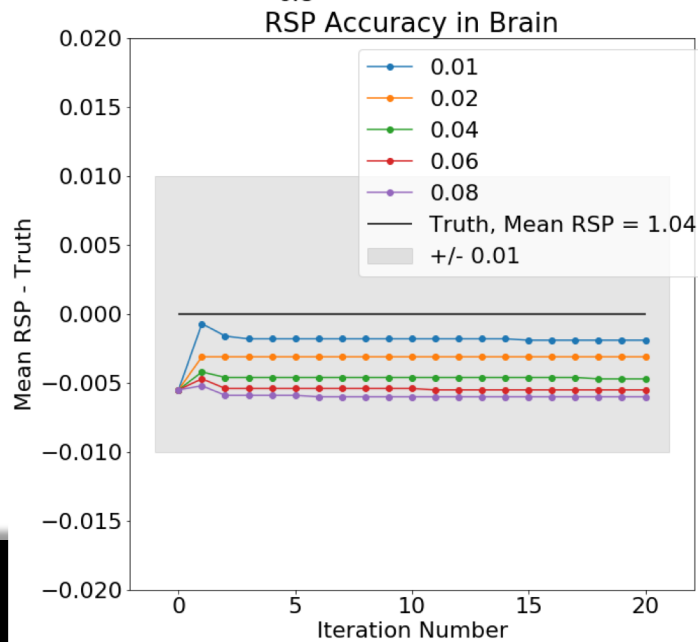
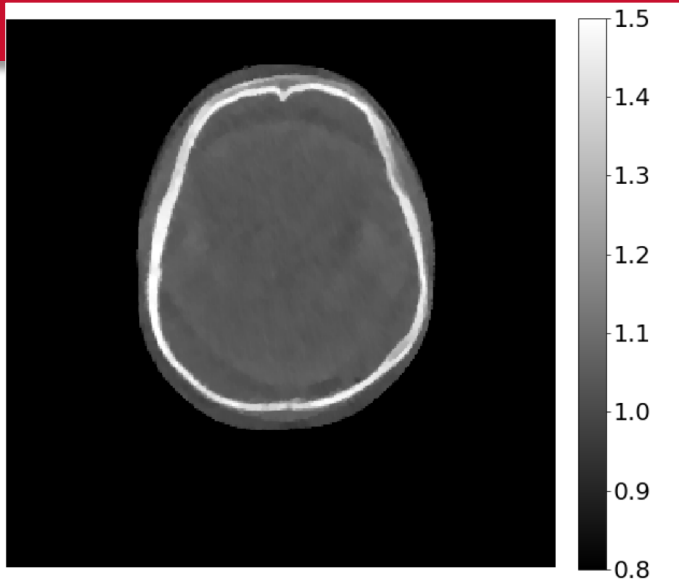
Spatial Resolution



$$MTF(LP) = \frac{(Peak - Valley)_{LP}}{(Peak - Valley)_{LP=1 \text{ cm}^{-1}}}$$



Pediatric Head Phantom - Brain



Conclusions



- Within the range of relaxation parameters tested, the RSP accuracy is +/- 0.01 for all CIRS materials and is not sensitive to relaxation parameter.
- CNR was measured to be 20 for Brain, 250 for Cortical Bone, and 400 for Sinus in the custom RSP phantom with $\lambda = 0.01$
- Spatial resolution of 5 lp/cm was measured for the line pair phantom with $\lambda = 0.08$
- There is a tradeoff between noise and spatial resolution.
 - Lower relaxation parameter shows lower noise, higher CNR
 - Higher relaxation parameter shows better spatial resolution

Future work



- Expand relaxation parameter range
- Repeat with DROP
- Repeat with half the total number of proton histories
- Suggestions?

Acknowledgements



- George Coutrakon
- Caesar Ordoñez
- Nick Karonis
- Reinhard Schulte
- Robert Johnson