

# Development of NTCP Models for Proton Therapy

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Original Article

Lyman–Kutcher–Burman normal tissue complication probability modeling for radiation-induced esophagitis in non-small cell lung cancer patients receiving proton radiotherapy

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# Outline

- Overview some proton NTCP model development works in MDACC based on the MDACC's proton outcome data
- Difference of photon and proton NTCP model: esophagitis modeling in NSCLC patients
- Importance of the “better” model for the model based treatment selection
- Role of advanced machine learning model in the model development
- Impact of variable RBE on the model development
- Summary

# NTCP model development in MDACC

Radiation pneumonitis for both proton and photon patients

## Lyman modeling

In the standard Lyman model, the NTCP is modeled using a cumulative normal distribution:

$$NTCP = \frac{1}{2\pi} \int_{-\infty}^t e^{-u^2/2} du \quad (1)$$

where  $t$  is given by:

$$t = \frac{D_{eff} - TD_{50}}{m \times TD_{50}} \quad (2)$$

The parameter  $TD_{50}$  represents the dose corresponding to 50% probability of the given complication,  $m$  is proportional to the inverse slope of the dose-response curve, and  $D_{eff}$  is the effective dose to which the entire volume is exposed:

$$D_{eff} = \left( \sum D_i^{1/n} \times v_i \right)^n \quad (3)$$

$$RMSD = D_{eff(n=0.5)} = \sqrt{\sum D_i^2 \times v_i}$$

Clinical Investigation

## Validation of Effective Dose as a Better Predictor of Radiation Pneumonitis Risk Than Mean Lung Dose: Secondary Analysis of a Randomized Trial

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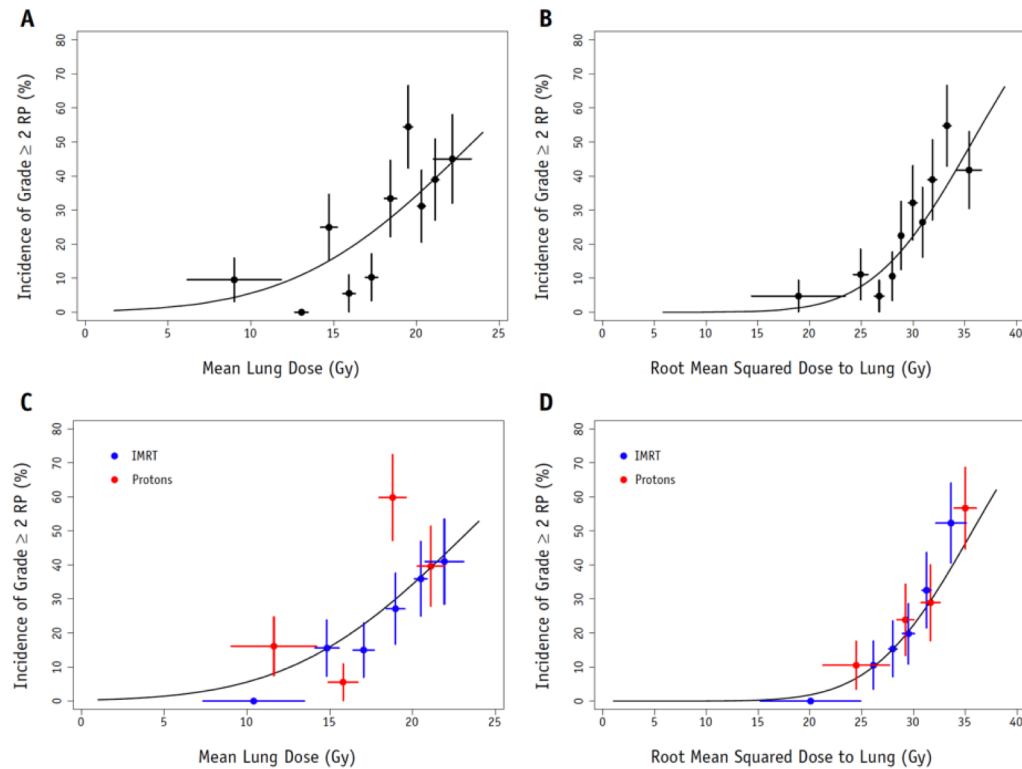
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**Table 1** Parameter estimates of the generalized Lyman model for grade  $\geq 2$  RP risk using the effective-dose with fitted  $n$  (left), mean lung dose (with  $n$  fixed at 1) (middle), or RMSD (with  $n$  fixed at 0.5) (right)

Parameter	Estimate	95% CI	Estimate	95% CI	Estimate	95% CI
	Effective dose model		Mean lung dose model		RMSD model	
$TD_{50}$ (Gy)	35.7	23.8-47.6	23.4	20.0-26.8	34.8	32.1-37.1
$m$ (1/Gy)	0.21	0.11-0.31	0.36	0.22-0.51	0.22	0.13-0.30
$n$	0.48	0.20-0.76	1	NA	0.5	NA
$\mu$	1.38	1.20-1.56	1.38	1.20-1.56	1.38	1.20-1.56
$\sigma$	0.61	0.49-0.75	0.61	0.49-0.75	0.61	0.49-0.75

*Abbreviations:* CI = confidence interval;  $m$  = proportional to the inverse of the slope of the dose-response curve pertaining to the given complication;  $n$  = parameter that affects relative weighting of different dose levels; NA = not applicable ( $n$  fixed in model fit); RMSD = root mean squared dose; RP = radiation pneumonitis;  $TD_{50}$  = tolerance dose corresponding to 50% probability of the given complication (radiation pneumonitis);  $\mu$ ,  $\sigma$  = parameters determining the shape of the time distribution (latency) over which RP occurs in the absence of censoring.

# The radiation pneumonitis for both photon and proton model can be described by RMSD model



No separate model needed

**Fig. 2.** Solid curves indicate predicted risk of grade  $\geq 2$  radiation pneumonitis from fits of the generalized Lyman model using mean lung dose ( $n = 1$ ; A and C) or root mean squared dose ( $n = 0.5$ ; B and D) as the dosimetric parameter. Plotted symbols represent groups of 20 to 21 patients each, with location on the abscissa indicating the average dosimetric value per group,  $\pm 1$  standard deviation, and location on the ordinate indicating the Kaplan-Meier estimate,  $\pm 1$  standard error, of grade  $\geq 2$  radiation pneumonitis at 12 months.



# Generalized LKB model

- A feature of the LKB model is that toxicity is regarded as a binary endpoint and scored as “yes” or “no” for each patient. This approach does not take into account the fact that some patients without toxicity might have experienced toxicity with longer follow-up. Moreover, the standard Lyman model does not incorporate **nondosimetric** risk factors such as comorbidities and other patient characteristics.
- A generalization of the Lyman model incorporating **censored time-to-toxicity data** and nondosimetric patient factors

# Generalized Lyman model with covariates added

$$NTCP = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^t e^{-\frac{x^2}{2}} dx,$$

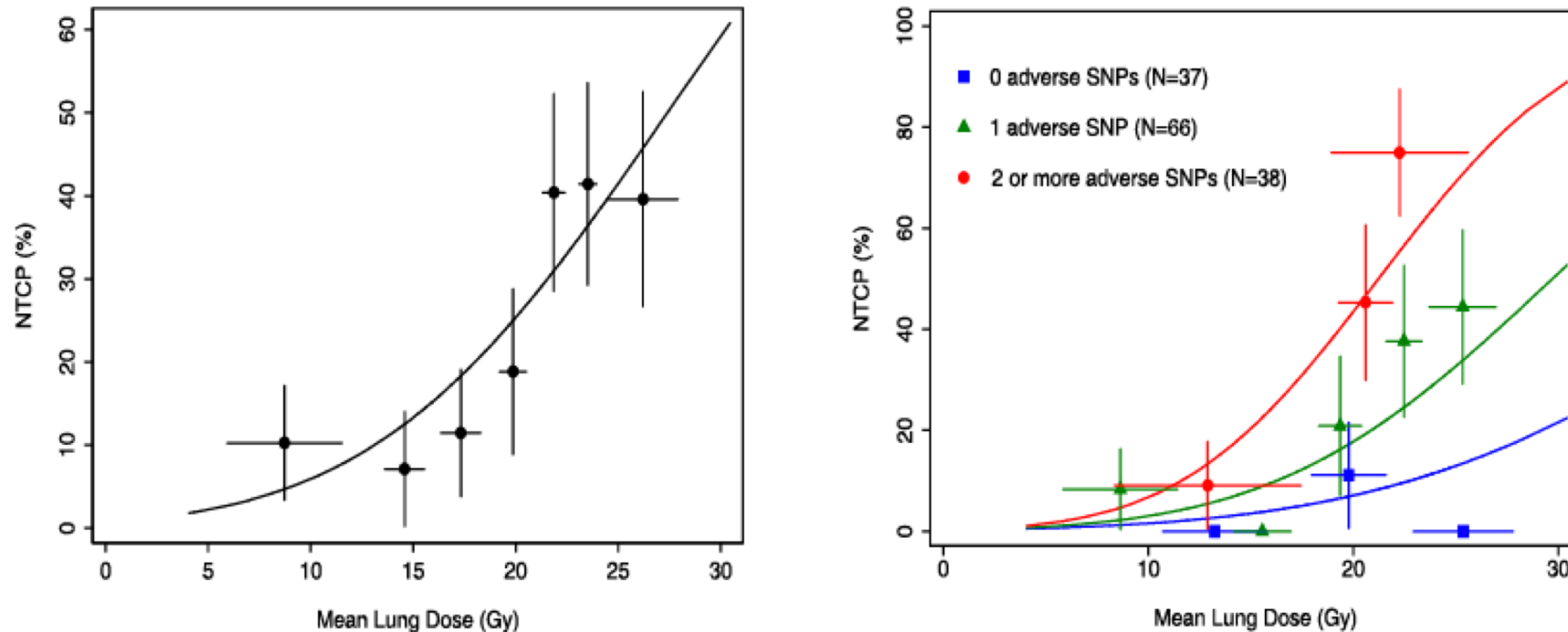
where  $t$  is equal to the following:

$$t = \frac{EUD * DMF_1 * \dots * DMF_k - TD_{50}}{m * TD_{50}}, \text{ and}$$

$$EUD = \left( \sum_i v_i D_i^{\frac{1}{n}} \right)^n,$$

The impact of the covariates such as SNPs, cTNT and other non-dosimetric factors are modeled by dose modifying factors  $DMF_i, \dots, DMF_k$ . The dose modifying factors are calculated as  $DMF_i = \exp(-\delta_i Y_i)$  where  $\delta_i$  is the fitting parameters and  $Y_i$  represents the non-dosimetric factors. We will first model the non-dosimetric factors  $Y_i$  as the binary variable. For the continuous variables such as cTNT, we will first do the threshold analysis can convert them into binary variable.

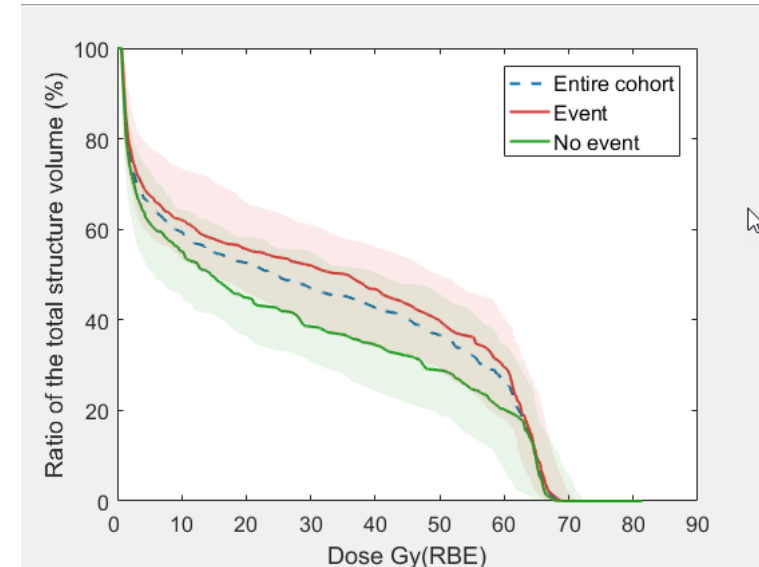
# Importance of incorporating non-dosimetric factors into Model



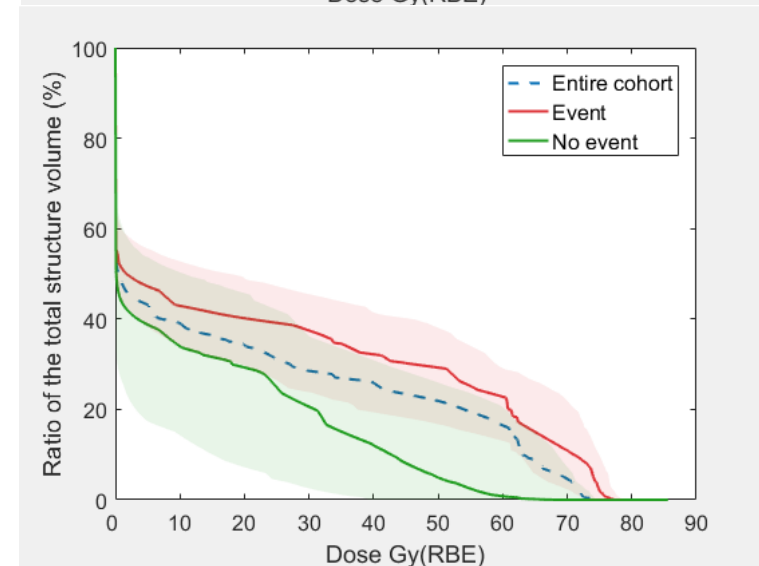
**Figure 7.** Incorporating SNP into NTCP model significantly improved predictive power for radiation pneumonitis. (left) MLD model, (right) number of risk SNP incorporated into the MLD model

# Esophagitis in NSCLC patients receiving PSPT

- 328 patients PSPT alone or with concurrent chemotherapy
- 50-82.5 Gy (RBE)
- Physician evaluation CTCAE 3.0
- Endpoint of the study: grade  $\geq 2$  esophagitis within 6 months from the first treatment
- Grade 2-3 136 patients (41.5%)
- Grade 4-5 0 patients



IMRT



PSPT

# Esophagitis in NSCLC patients receiving PSPT

- Lyman-Kutcher-Burman (LKB) modeling

$$\text{NTCP} = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^t e^{-\frac{x^2}{2}} dx,$$

$$t = \frac{\text{EUD} - \text{TD}_{50}}{m * \text{TD}_{50}},$$

$$\text{EUD} = \left( \sum_i v_i D_i^{\frac{1}{n}} \right)^n$$

- 3 Parameters  $n, m, \text{TD}_{50}$
- Using maximum likelihood estimates

$$\text{LL}(n, m, \text{TD}_{50}) = \sum_{p=1} \ln(\text{NTCP}(n, m, \text{TD}_{50})) + \sum_{p=0} \ln(1 - \text{NTCP}(n, m, \text{TD}_{50}))$$

**n=0.24 Smaller volume effect**

	<b>PSPT</b>	<b>3DCRT<sup>1</sup></b>	<b>IMRT<sup>2</sup></b>
n	<b>0.24</b>	0.44	1.04
m	<b>0.51</b>	0.32	0.65
TD <sub>50</sub>	<b>44.83</b>	51	32.84

MDACC own IMRT data

	<b>n</b>	<b>m</b>	<b>TD50</b>
<b>IMRT</b>	0.69	0.93	27.56

- Chapet, O. *et al. Radiother. Oncol.* **77**, 176-181 (2005).
- Wijnsman, R. *et al. Radiother. Oncol.* **117**, 49-54 (2015).

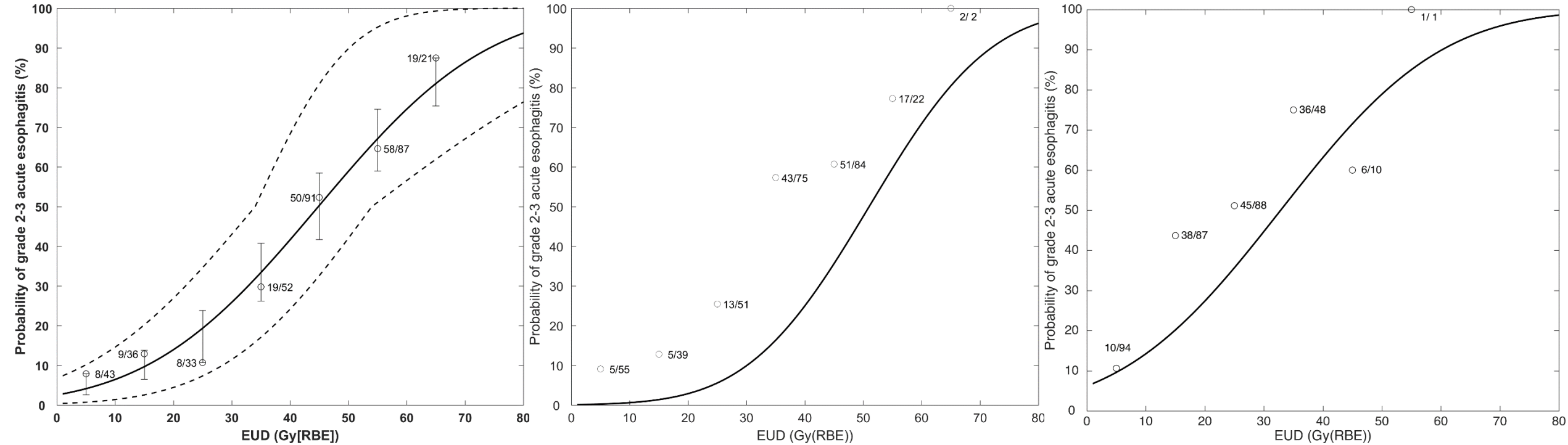
# Esophagitis in NSCLC patients receiving PSPT

Predicted probability versus observed outcome  
Photon-based models underestimated the NTCP

### PSPT

### 3DCRT

### IMRT



# Selection of patients benefit from proton therapy based on the NTCP model



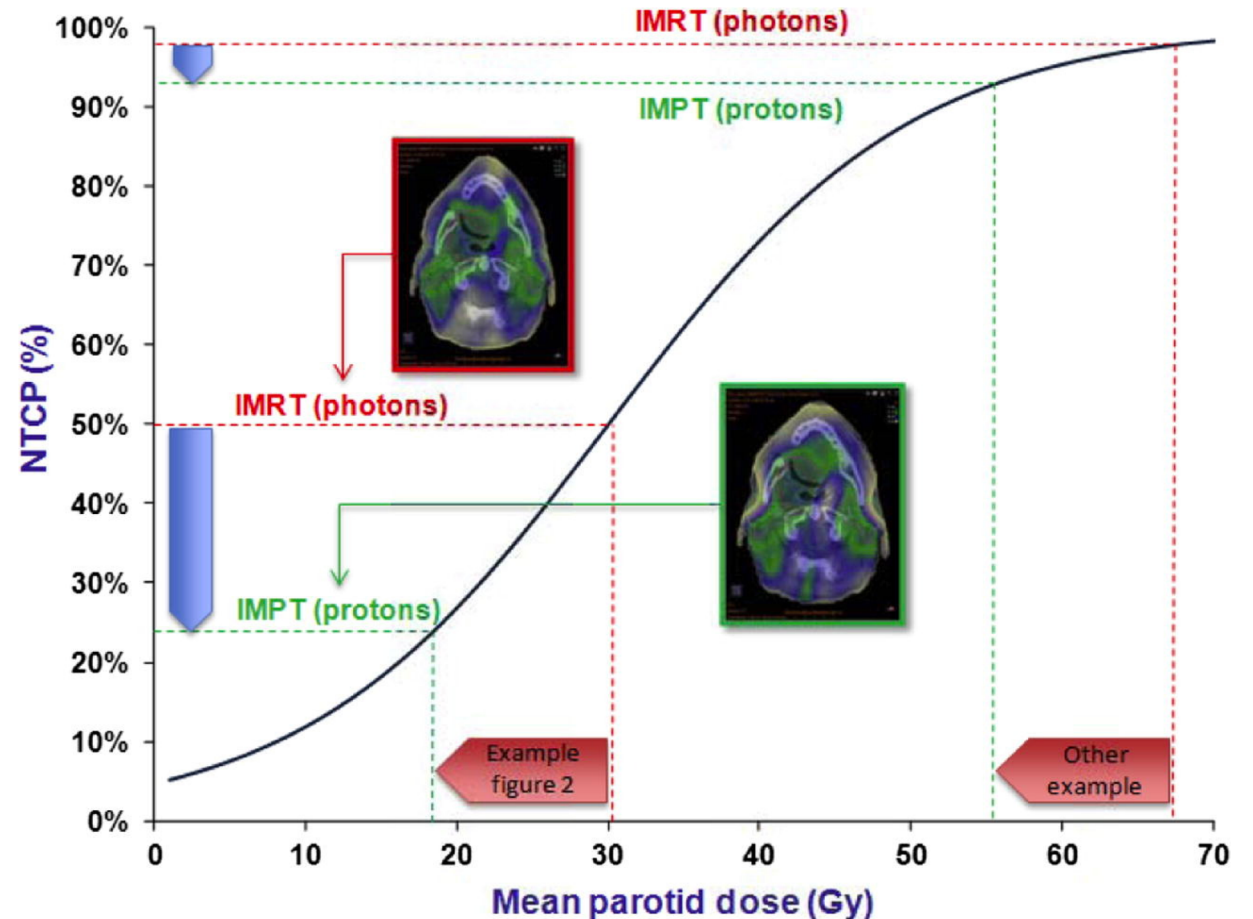
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Proton radiotherapy

Selection of patients for radiotherapy with protons aiming at reduction of side effects: The model-based approach

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# Virtual patient selection study based on the lung randomized trials

- 53 out of 57 patients treated with PSPT from lung IMRT/Proton randomized trials was selected for study
- 37 out of 53 patients developed greater than grade 2 esophagitis. (70%)
- Each patient has two optimized plans: PSPT plan and IMRT plan
- If using the NTCP model developed based on IMRT data (Wijsman, R. *et al. Radiother. Oncol.* **117**, 49-54 (2015)., if criterion of selection patient for proton treatment is that proton plan improves NTCP by 1%, 2%, 5%, 32, 30, 20 patients will be selected for proton treatment, however the rates of esophagitis are 69%, 70% and 75%
- If using NTCP model developed using proton data for proton plan and NTCP model developed using IMRT data for IMRT plan, if criterion of selection patient for proton treatment is that proton plan improves NTCP by 1%, 2%, 5%, 7, 5, 4 patients will be selected for proton treatment, the rates of esophagitis are 43%, 40% and 25%

**Using a not accurate model dose not help for the patient selection**

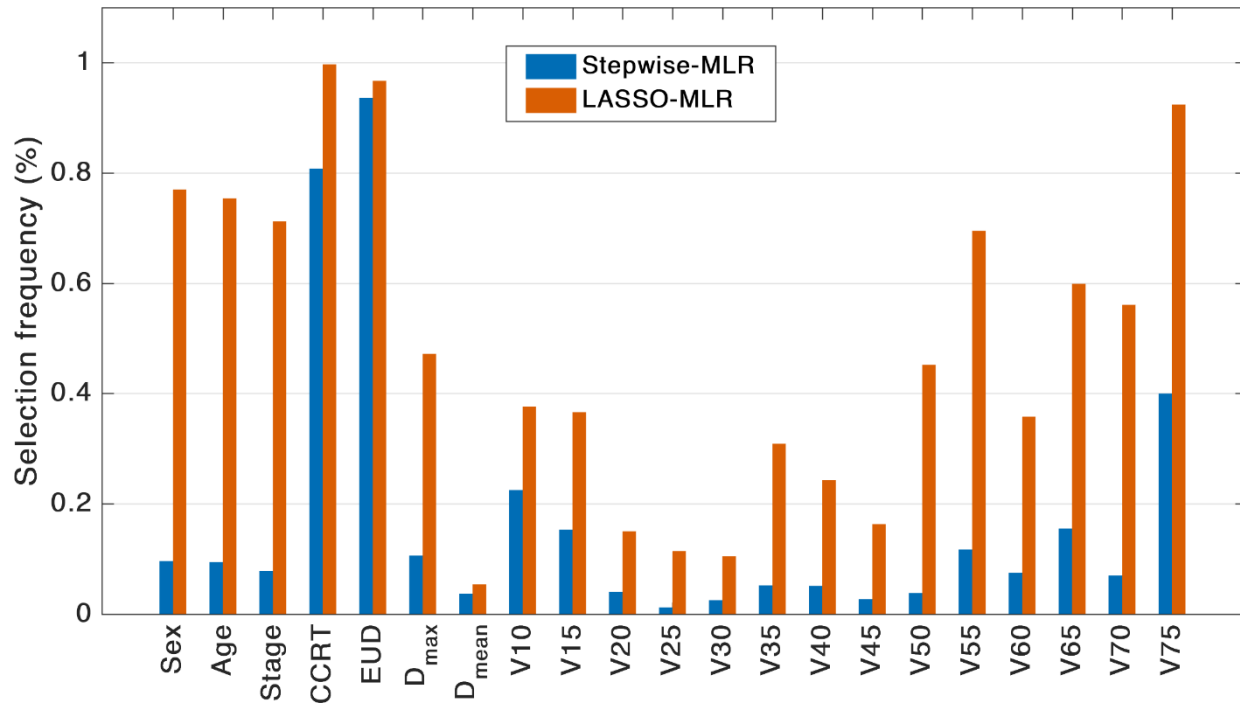


# Will advanced modeling technique help?

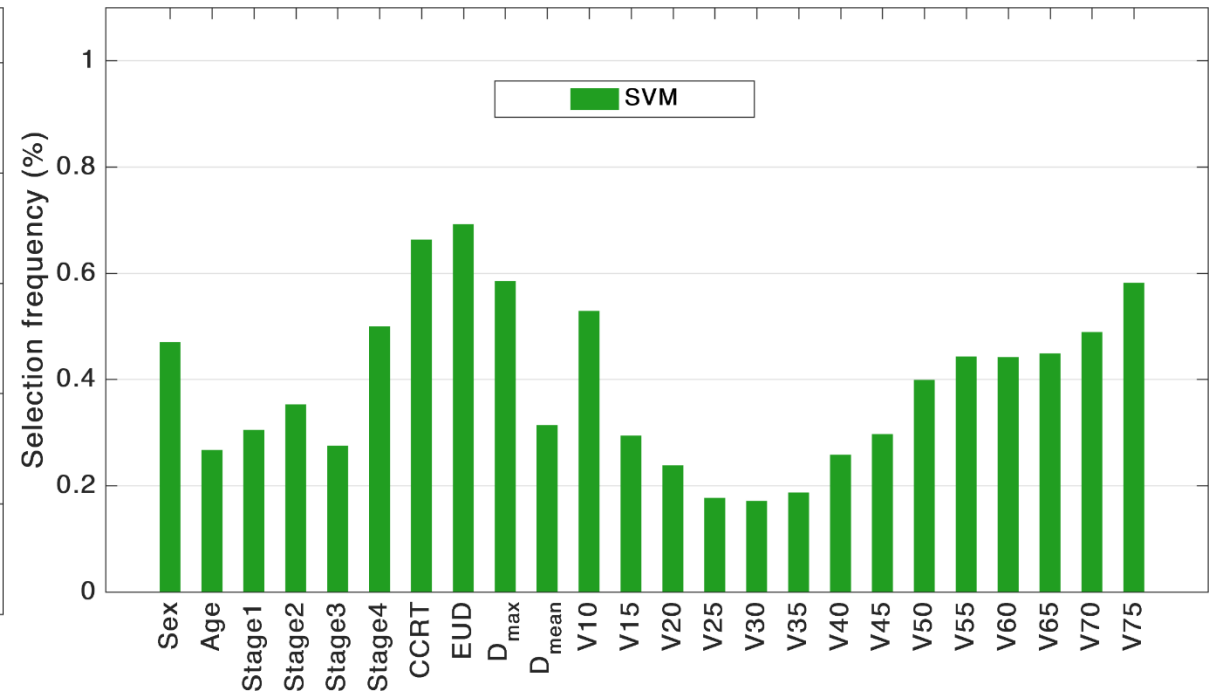
- Generalized LKB model accounting for the clinical factor (with or without Chemotherapy )
- Multivariable logistic regression model (Stepwise, LASSO feature selection)
- Machine learning-SVM

# Feature selection

## Multivariable logistic regression



## SVM



# Parameters and coefficients

Models	Parameters/Features	Coefficients/Formula
sLKB	$n, m, TD_{50}$	$n = 0.24, m = 0.51, TD_{50} = 44.83 \text{ Gy (RBE)}$
gLKB	$n, m, TD_{50y}, TD_{50n}$	$n = 0.23, m = 0.54, TD_{50y} = 42.17 \text{ Gy (RBE)}$ $TD_{50n} = 57.84 \text{ Gy (RBE)}$
Stepwise-MLR	CCRT, EUD	$\log\left(\frac{p}{1-p}\right) = -3.5845 + 0.8505 * \text{CCRT} + 0.0664 * \text{EUD}$
LASSO-MLR	CCRT, EUD, V75	$\log\left(\frac{p}{1-p}\right) = -3.2766 + 0.7913 * \text{CCRT} + 0.0573 * \text{EUD} + 0.0438 * \text{V75}$
SVM	CCRT, EUD	$C=2^{15}, \delta=2^{-13}$

# Will advanced modeling technique help?

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Models	AUC	LL	$\Delta$ AIC
sLKB	0.785 (0.783)*	-178.55	--
gLKB	0.799 (0.796)*	-174.46	6.18
Stepwise-MLR	0.800 (0.797)*	-174.20	10.70
LASSO-MLR	0.803 (0.799)*	-172.48	12.14
SVM	0.799 (0.784)*	-174.45	9.59

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\* Apparent performance(optimism-corrected performance

# Biological uncertainty

- $S = \exp(-\alpha d - \beta d^2)$
- $S = \exp(-\alpha d)$
- $\alpha = \alpha_0(1 + cLET)$  LET < 30 keV/um
- $BD = -\log(S)/\alpha_0 = (1+cLET)d$
- $cLET*d$ : additional biological dose due to LET effect
- $c = 0.04$

10-cm range 5-cm SOBP LET=2.5 keV/um RBE=1.1

Bragg peak LET=7.5 keV/um RBE=1.3

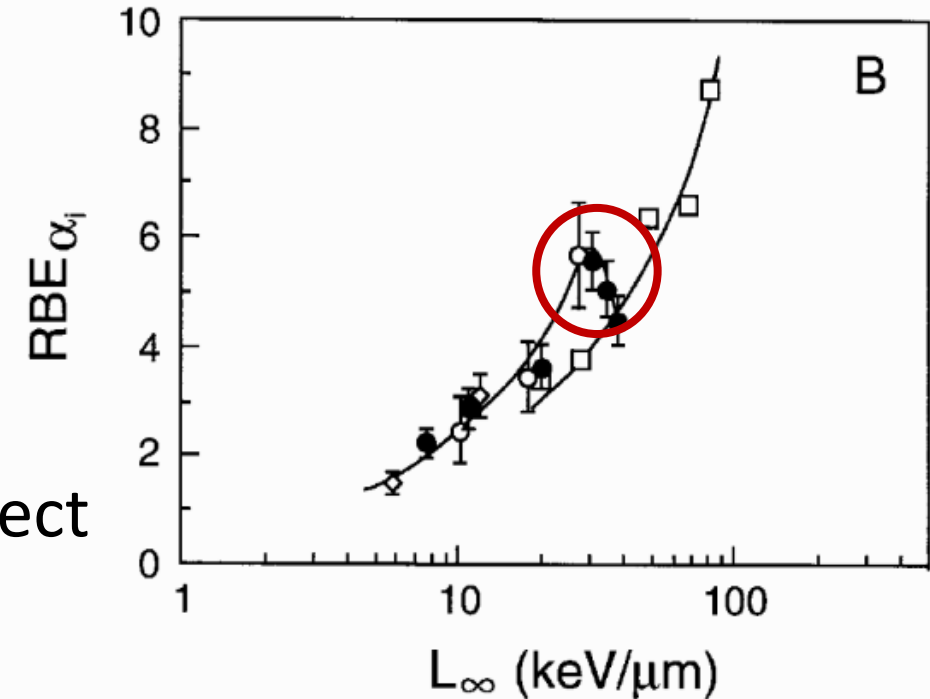


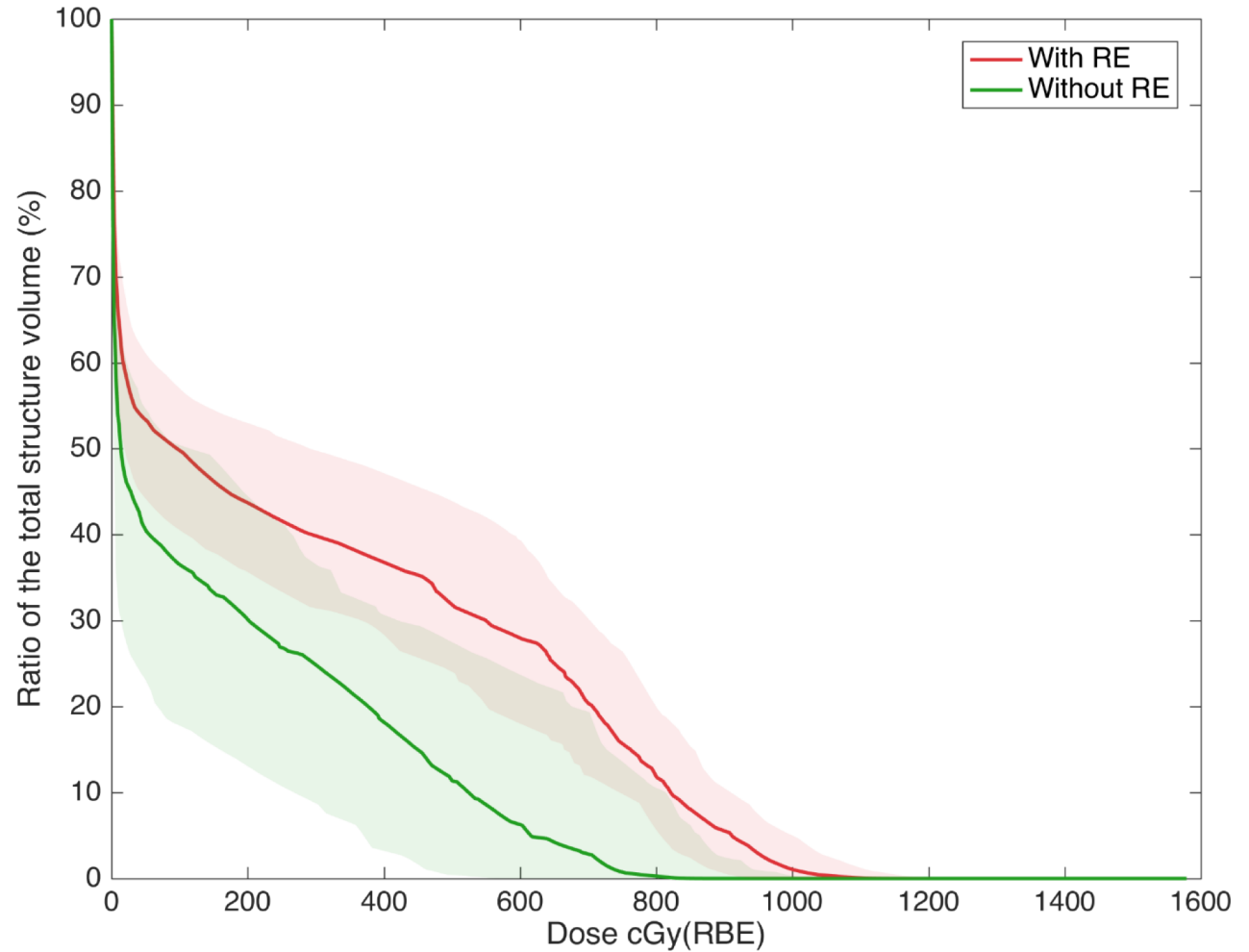
Figure 2. (A) inactivation cross sections ( $\sigma_i$ ) and (B)  $RBE_{\alpha}$  derived from the initial slope ratio ( $\alpha_p/\alpha_x$ ), as a function of LET. (●) protons (present data); (◇) protons (Perris *et al.* 1986); (○) protons (Folkard *et al.* 1996); (□) helium ions (Cox *et al.* 1977).

# Have we underestimated NTCP using RBE=1.1 ?

- 114 patients
- One treatment course
- Prescription 60-87.5 Gy (RBE)
- Plan recalculated by Monte-Carlo-like fast dose calculator
- Biological uncertainty:  $0.04\text{LET}_d * D$

# Have we underestimated NTCP using RBE=1.1 ?

	<b>Grade 0-1</b>	<b>Grade 2-3</b>	<b>P Value</b>
DLmax	8.71 ± 3.94	11.33 ± 2.28	<0.001
DLmean	1.87 ± 1.44	3.07 ± 1.06	<0.001
DL1cc	6.47 ± 3.54	9.24 ± 1.94	<0.001
DL2cc	5.77 ± 3.46	8.74 ± 1.90	<0.001
DL5cc	4.43 ± 3.25	7.62 ± 1.92	<0.001



# Have we underestimated NTCP using RBE=1.1 ?

Multivariable logistic regression models with or without DL

<b>Dose</b>	<b>DL</b>	<b>AUC</b>	<b>LL</b>	<b>Log likelihood ratio test <i>p</i> value</b>
D2cc, V75		0.846	-54.34	--
D2cc, V75	DLmax	0.841	-54.33	0.89
D2cc, V75	DLmean	0.850	-53.65	0.24
D2cc, V75	DL1cc	0.839	-54.33	0.89
D2cc, V75	DL2cc	0.838	-54.34	1
D2cc, V75	DL5cc	0.842	-54.25	0.68



# Summary

- Proton dose distribution pattern and photon dose distribution pattern are different. This required us to develop proton specific NTCP model
- It should be cautious to use NTCP model developed using photon data to perform the model based patient selection for proton treatment
- LKB model and generalized LKB model is not worse than the current most up to date machine learning approach
  - Data is not large enough
- It is time for the proton therapy community to work together to share the data and develop proton “QUANTEC”